

Empirical analysis of density optimization models for supercapacitors from a statistical perspective with

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Abstract: When compared to other kinds of energy storage devices, supercapacitors are more suited for wider deployment because they have a longer cycle life, quicker charge and discharge operations, and a higher safety rating. This makes them ideal for use in a variety of applications. Because of their relatively low energy density, supercapacitor devices have limited use in the real world. Therefore, the purpose of this article is to explain the factors that have an effect on the energy density of supercapacitors and to propose alternate techniques for boosting that energy density by optimizing capacitance, operating voltage, and several other parameters. This article provides a forward-looking view on the most noteworthy advancements regarding high-energy-density supercapacitors and delivers that perspective in the form of contextual observations. This will assist circuit designers to identify optimal models for different use cases. This text also compares the discussed models in terms of their efficiency, scalability, operational speed, deployment cost and complexity levels. This comparison will assist readers to identify optimal models for their performance-specific use cases. To further simplify the process of model selection, this text proposes evaluation of a novel Super Capacity Optimization Rank Metric (SCORM) that combines these metrics. This evaluation assists in identification of optimization models for high-speed, low complexity, high efficiency, high scalability and low-cost scenarios.

Keywords: Super, Capacity, Energy, Density, Cost, Delay, Scalability, Speed, Complexity, Scenarios

1. Introduction

When the scale of the energy and environmental concerns we currently confront is taken into consideration, the development of green fuel cells and techniques is no longer a luxury but rather a need. Either supercapacitors or lithium-ion batteries make up the vast majority of the energy storage technologies that are commercially available today [1,2]. As a result of the lithium-ion battery's (or "LIB") high energy density [3,4], it has found employment in a broad range of real-world applications, such as powering portable electronic gadgets and

electric vehicles (EVs). An electric car can run over 310 miles at a time. Because it might take several hours to fully charge an electric vehicle's battery, these cars have a restricted driving range. When choosing an energy storage system, large-scale applications like electric vehicles need extra study and care (EVs). The ability of supercapacitors to charge quickly, their high power density, the broad temperature range in which they may operate, and their safety [5] are all advantages of using these devices. The average time it takes for a supercapacitor to charge is anything from a few seconds to a few minutes, and it may cycle for

as many as 100,000 times without suffering significant performance degradation. As a consequence of these developments, supercapacitors have emerged as the most cutting-edge and advanced kind of energy storage technology that is now accessible. Despite this, the energy density that they possess is not very great. The traditional supercapacitors have a limit of 10 watt-hours per kilogram for the amount of energy that can be stored in them [3]. Because of their high-power density and relatively fast discharge time, supercapacitors are currently exclusively put to use as starters for electric vehicles and as door switchers in airline cabins. As EV power sources, supercapacitors are preferred to LIBs due to the fact that their cycling life is usually 2,000 cycles, which is equivalent to between 5 and 6 years if the device is charged once per day (Table 1). Because of their low upfront cost, supercapacitors are quickly becoming one of the most promising candidate technologies for use in electric vehicle power sources.

On the other hand, the life expectancy of supercapacitors is far longer than 10 years. Additionally, supercapacitors may be refilled in a matter of minutes, which is a much shorter amount of time compared to the amount of time required to replace oil. The fundamental restriction of the technique is the needed operating range (energy density) for usage in electric cars, which is at least one hundred kilometres. This range must be satisfied. It is reasonable to assume that each kilogram has more than one-hundred-watt hours of usable energy. Because of this, there is no limit to the distance that you are able to go, and the amount of time that is necessary to charge your gadget is almost non-existent. The use of supercapacitors with the same performance as LIBs has the potential to significantly increase the range of electric vehicles. From this vantage point, we are going to present a concise review of the most recent breakthroughs that have

enhanced the energy density of supercapacitors, as well as the most critical obstacles that still need to be handled before we can produce high-performance supercapacitors. In addition, we stressed the relevance of the link between the energy density and essential routes, such as the capacitance and operating voltage. This is because we believe that this relationship is directly proportional to the efficiency of the device. We hope to provide an overview of recent advancements in high-energy-density supercapacitors and identify pathways for developing further advancements in these devices by providing a summary of key elements such as surface area, pore size, surface functional groups, high-voltage electrolytes, and various supercapacitor device configurations. In doing so, we hope to provide an overview of recent progress in high-energy-density supercapacitors. Then we will be able to provide you with a concise summary of the most recent developments in high-power supercapacitors.

A survey of such optimization models is discussed in the next section of this text, which is followed by an empirical analysis of these models, and their comparison in terms of different evaluation parameter sets. Finally, this text is concluded with observations and recommendations to improve performance of these models under different scenarios.

2. Detailed review of density optimization models for super-capacitors

Researchers have developed a slew of supercapacitor optimization models, each with its own set of internal working characteristics. Supercapacitors, a revolutionary form of energy storage device, for example, are extensively employed in many energy storage applications owing to benefits like as rapid charging and discharging, high power density, a broad working temperature range, and longer cycle

life. This is addressed by experts in supercapacitor optimization work in [1]. However, the degradation and failure of supercapacitors in large-scale applications would have a significant influence on the whole system's operation. To optimize efficiency, reduce equipment damage, and guarantee that supercapacitors be changed in a timely way before they lose their efficacy, it is critical to precisely forecast how long they will survive. This article compares model-based and data-driven (MDT) techniques for determining the remaining usable life of supercapacitors in order to serve as a reference for future study in this field. It also describes the peculiarities of the various approaches and anticipates future advances.

According to studies presented by optimization experts in [2] supercapacitor electrodes constructed of activated carbon (AC) provide high energy and power capabilities since they have a larger surface area, greater conductivity, and the flexibility to change supercapacitor characteristics. Supercapacitors have piqued the attention of researchers due to their higher stability and faster charging/discharging rates than regular batteries. To boost the specific capacitance and energy storage capabilities of supercapacitors, GO/PPy/AC composite electrodes were created using a modified Hummers' process, a sacrificial template polymerization approach, and a hydrothermal method. The AC was made from *Ziziphus jujuba* seeds and *Prunus dulcis* shells. The capabilities of numerous electrodes were tested using a 6 M KOH electrolyte at varied current densities and scan speeds. The electrochemical characteristics of the electrodes were studied using differential analysis to determine whether the electrode material was acceptable. At varying current densities, the specific capacitances of the GO/PPy/ACPD (GPA) electrode were 1217.1, 456.67, 270.44, and 90.88 F, respectively. GO/PPy/ACPD has a

high specific capacitance of 1217.1 F. The higher electrochemical performance is due to increased surface area and specific capacitance.

Experts in supercapacitor design are exploring the state of charge (SOC) estimation of lithium batteries and supercapacitors in electric vehicle hybrid energy storage systems in [3]. The circuit models of lithium batteries and supercapacitors were developed using the energy storage principle of the electric vehicle composite energy storage system, and the model parameters were identified online using the recursive least square (RLS) method and the Kalman filtering (KF) algorithm, respectively. SOC was then computed in real time using both scented and unscented Kalman filtering techniques. Finally, the experimental platform for SOC estimation was built, and Matlab was used for computations and analysis. The experimental findings demonstrated that the SOC estimate results were very accurate, with an estimated error variation range of [0.94%, 0.34%]. In the situation of accurate total weighing and amount computation, the recursive least squares approach and the 2RC model are coupled to produce the best results for lithium batteries, and the estimate error is within the range of [1.16%, 0.85%]. The system is also very dependable and long-lasting.

The study in [4] goes into great depth on the development of high-density supercapacitor devices. A hierarchical structure of TiO₂ nanorod/MnO₂ ultrathin nanosheet core/shell nanocomposite arrays on a conductive substrate was constructed using two simple techniques: hydrothermal reaction and annealing progression. The use of these electrodes in high-performance supercapacitors has huge promise. The thickness of the MnO₂ shell in the hierarchical electrode material has been found to be readily adjustable by adjusting the concentration of the precursor aqueous solution. According to the findings of a cyclic

voltammetry (CV) test at a scan rate of 5 mV/s, the TiO₂ nanorod/MnO₂ ultrathin nanosheet developed as an electrode material may achieve the greatest electrochemical performance in terms of area-specific capacitance up to 34.79 mF/cm². Furthermore, after 1000 cycles of the cycle experiment test, the composited electrode demonstrated good stability, with a capacitance retention rate of about 91%.

In work offered by supercapacitor optimization experts in [5] a supercapacitor hybrid energy storage system is added to a wind-solar hybrid power producing system, which may greatly increase the system's energy storage capacity and output power. The technique in this work connects a distributed power producing system with a hybrid energy storage system by using a static reactive power compensation system and a conductance-fuzzy dual-mode control approach. The MATLAB/Simulink software is also used to generate the ideal configuration model for the wind-solar hybrid power generation system. The microgrid's output power to the wind-photovoltaic hybrid power generation system may be evaluated by modelling the optimization process for each system component. This study principally employs the static reactive power compensation system and the conductance-fuzzy dual-mode control technique to optimize the wind-solar hybrid power generation system. Simulations are run using the MATLAB tool to ensure the feasibility and consistency of the ideal system topology.

Work in [6] discusses how experts have improved supercapacitors. The positive electrode was constructed from manganese dioxide/gold/nickel foam, whereas the negative electrode was constructed from graphene or commercially available activated carbons (AC) (MANF). The impact of different negative electrode materials and negative/positive electrode mass ratios on the electrochemical

properties of the asymmetric supercapacitor were thoroughly investigated. The results suggest that the mass ratio of the negative/positive electrode has a substantial impact on the specific capacitance of the asymmetric supercapacitor. Charge balancing demonstrates that the negative to positive electrode's optimum mass ratio is somewhat lower than expected. However, the asymmetric supercapacitor using commercial AC as the negative electrode outperforms the one with graphene as the negative electrode in terms of specific capacitance and rate capability. The negative material has little effect on the cycle stability of an asymmetric supercapacitor. In the neutral Na₂SO₄ aqueous solution, the optimized asymmetric supercapacitor may also achieve an effective and optimum cell voltage of 1.8 V, as well as an efficient energy density at high power density. The device's positive electrode is a MANF composite, whereas the negative electrode is an AC.

According to studies detailed by optimization experts in [7], transition metal phosphides (TMPs) are appropriate battery-type electrodes for hybrid supercapacitors due to their high electrical conductivity and electrochemical activity. (HSCs). TMPs with fast kinetics and stable structures are difficult to produce, yet they are required for high-performance HSCs. Our Ni-Co-Mo-P (or Ni-Co-W-P) heterostructures exhibit a unique three-dimensional (3D) open shape and different electrical structures. According to DFT calculations and electrochemical measurements, the addition of Mo/W to NiCoP results in a perfect nanostructure, excellent conductivity, a large number of reaction active sites, and better reaction kinetics. The developed Ni-Co-Mo-P heterostructure outperforms its NiCoP and NiCo-W-P counterparts in terms of areal capacity and cycle stability. a Ni-Co-Mo-P/activated carbon (NCMP AC) device capable of high energy and power density,

demonstrating the Ni-Co-Mo-P heterostructure's potential as part of an energy conversion and storage system. Because of its greater adaptability, the all-solid-state Ni-Co-Mo-P/AC device is an excellent choice for wearable energy storage devices.

According to research published in [8], supercapacitors are a breakthrough kind of high-performance nanoengineered device that combines the large capacity of batteries for electric energy storage with the capacity of dry capacitors for extremely rapid charging or discharging rates. Supercapacitors can therefore meet the high energy- and power-density needs of a variety of portable electronic devices and biosensors. This research looked at the possible use of various carbon nanoforms, metal oxides or hydroxides, chalcogenides, carbides, and phosphates, as well as organic redox species, conductive polymers, metal-organic frameworks, MXenes, and other nanomaterials in innovative supercapacitors. Researchers investigated the efficacy of several ways for increasing the volumetric capacitance, power density, and charge or discharge cycle stability of micro-supercapacitors made from these materials (MSCs). Special attention has been paid to the development of micro-supercapacitors that can be integrated with flexible microcircuits for wearable and implantable biomedical devices, remotely rechargeable sensors, microprocessor-controlled data processing chips, biomorphic computing, smart phone communication, military, automotive, and emerging technologies. A variety of design and manufacturing processes for MSCs have been compared, including femto-laser writing, photolithography, screen printing, stamping, inkjet printing, mask patterning, and others. MSCs have been recognized for their fascinating potential.

According to studies referenced by high-density supercapacitor manufacturers in [9], photo-

rechargeable supercapacitors are appropriate energy storage devices, particularly for solar cells that generate electricity primarily during daylight hours. Supercapacitors have a low energy density due to a lack of redox-active sites, restricted electrolyte accessibility at the electrodes, and charge loss during the charge transfer from solar cells to the supercapacitor. In this application, an organic-inorganic hybrid electrode with electrolyte accessibility is used to boost the energy density of the supercapacitor by merging $\text{Ti}_3\text{C}_2\text{Tx}$ pseudo-capacitance with C-O active centres. According to calculations utilizing the density functional theory, covalent cross-linking of organic molecules changes the charge density redistribution of $\text{Ti}_3\text{C}_2\text{Tx}$, enhances ion absorption and storage, and increases the energy density of the supercapacitors (DFT). Based on these DFT simulation findings, hybrid electrodes are successfully constructed by covalently cross-linking pseudo-capacitors $\text{Ti}_3\text{C}_2\text{Tx}$ with anthraquinones such as 1-hydroxyanthraquinone (HA) or 1-amino-4-bromoanthraquinone-2-sodium sulfonate using p-phenylene diisocyanate. $\text{Ti}_3\text{C}_2\text{Tx}$ -HA hybrid electrodes have a high specific area (2532.5 mF cm^2), excellent ion absorption storage, and long-term stability. The asymmetric supercapacitor has a respectable area specific capacity (1686.72 mF cm^2 at 0.25 mA cm^2) and energy density (599.72 mWh cm^2 at a power density of 200 mW cm^2). These high-energy-density supercapacitors are paired with perovskite solar cells to make photo-rechargeable supercapacitors with rapid energy storage.

The expansion of flexible and wearable electronics needs the deployment of efficient energy storage technologies, according to a study published in [10] by experts in supercapacitor optimization. Researchers are interested in the better energy storage qualities of metal ion batteries and electrochemical

capacitors, such as their high energy and power densities and longer cycle lifetimes. The stiffness and toxicity of metal-ion batteries, as well as their flammability and low power density owing to organic electrolytes, all represent significant barriers to their usage in wearable devices. In contrast, supercapacitors employ aqueous electrolytes and are a safer option for wearable applications. Metal-organic frameworks (MOFs), a growing crystalline substance, are among the modern electrode materials utilized in energy storage systems. These materials have exceptional properties such as a large surface area, a 3D porous and adaptable structure, permeability to foreign objects, and others. Incorporating conductive components into their composites may assist to compensate for the weak conductivity of the basic MOFs. Transition metal-based MOF electrodes are ideal for wearable and flexible supercapacitors due to their benign nature, low cost, high energy and power density, and outstanding stability. This review focuses on supercapacitor technology, types, and efficiency-controlling factors, as well as new findings in the field of non-noble metal-based MOFs electrode materials for the development of supercapacitors by synthesizing the MOFs, MOFs derived materials, and composites by various fabrication schemes, as well as the challenges posed by the use of MOFs and their promising solutions.

This is mentioned by supercapacitor optimization experts in their work in [11]. Concerns about the safety issues associated with flammable organic electrolytes in alkali-ion batteries, as well as the necessity for high energy density and power density in a single device, prompted researchers to investigate aqueous multivalent metal ion hybrid supercapacitors. ZIHSCs have a high theoretical capacity, a low standard potential, and great aqueous electrolyte safety. This paper addressed and detailed the most recent advancements in

ZIHSCs. On the electrochemical performance of ZIHSCs, the impacts of cathode, anode, electrolyte, and other improvements have been observed. Multifunctionality and integration, as well as mechanism studies employing different ex-situ and in-situ methodologies, are also shown. Further in-situ characterization approaches are recommended to further understand the electrochemical mechanism of ZIHSCs. It is expected that ZIHSCs will ultimately develop practical applications with higher power output and active material utilization rates, as well as more functioning ZIHSC assemblies.

According to studies iterated by optimization experts in [12], an aqueous electrolyte may give excellent performance and a wide operating voltage. Aqueous electrolytes get more attention in supercapacitor applications than other electrolytes due to their safety, affordability, and lack of toxicity (such organic solvents and ionic liquids). Hydrothermally generated aniline 2-sulfonic acid (ASA) and poly-pyrrole (PPy) electrodes on carbon felt (CFt) for use in supercapacitor applications. researchers investigate the effect of ASA concentration on PPy polymerization. An asymmetric supercapacitor (ASC) with a graphite plate and a high operating voltage of 3.0 V is also included in the 3 M KCl. After 5000 cycle-life testing, the material CFt/PPy/ASA (0.02)/GP has a high specific capacitance value of 902.9 F g⁻¹ at 5 mV s⁻¹ and a capacitance retention of 93.6%. The finished ASC has an ultrahigh energy density of 1005 Wh kg⁻¹ and a power density of 3000 W kg⁻¹ with a current density of 2 A g⁻¹. The capacity of the supercapacitor to function is affected by ASA concentration, as shown in many application situations.

Professionals in supercapacitor design go into considerable detail about this in their work [13]. To satisfy the needs of societal power growth, it is critical to develop unique, ecologically

acceptable energy storage systems. Supercapacitors have received a lot of interest as a new kind of energy storage technology due to its high energy density, high power density, rapid charging and discharging rates, and prolonged cycle life. The electrode material has a considerable impact on the electrochemical performance of supercapacitors. Metal-organic frameworks (MOFs) and their derivatives have lately been investigated as supercapacitor electrode materials by researchers. This study addresses the synthesis of conductive, monometallic, and bimetallic MOFs, as well as their variants (VMOF), for usage in supercapacitors. The problems MOFs confront in the realm of supercapacitors, as well as their future development potential, are also discussed.

According to research by high-density supercapacitor manufacturers [14], energy storage has become the most significant topic of study in the twenty-first century due to the increasing requirement for energy to fulfil a range of modern needs. Supercapacitors (SCs) are energy storage devices that can power a range of electronic gadgets, electric and hybrid autos, as well as cutting-edge military and space equipment. The electrode materials have a considerable impact on the electrochemical performance and stability of these energy devices. As a result, it is critical to develop materials that are dependable, lightweight, and flexible enough to be employed in a wide range of applications. MoS₂, which exhibits excellent chemical and physical properties, is one of the most well-known two-dimensional nanomaterials in recent years. The primary purpose of this research is to better understand the electrochemical performance, properties, and synthesis of MoS₂ and its composite-based functional materials. The potential applications of MoS₂ indicate that there are still a lot of fields that need study and development.

The study advised by supercapacitor optimization experts in [15] looks at The electrochemical effectiveness of carbon-based supercapacitors is determined by surface area, conductivity, and material structure. The long, fibrous stalk of *Sussurea involucrata* was chosen as the novel kind of carbon source in order to synthesize carbon compounds with an effective structure. Chemical activation with KOH may successfully create highly ordered micropores activated carbon (HOMAC) materials. The generated HOMAC has a high specific surface area of 2692 m² g⁻¹ and a pore volume of 1.14 cm³ g⁻¹. The constructed HOMAC-based electrode has a high specific capacitance of 379 F with H₂SO₄ aqueous electrolyte and remarkable cyclic stability (the capacitance retention is 95% after 10000 cycles at a current density of 1 A g⁻¹). Furthermore, the operating voltage window of the 2-electrode system in 1 M Na₂SO₄ electrolyte may be expanded to 0-1.8 V. The symmetric supercapacitor has a power density of 180.03 W kg⁻¹ and a high energy density of 33.91 Wh kg⁻¹. These outstanding results are attributable to the activator KOH's ability to create well-ordered, high surface area microporous structures. researchers also discussed the relationship between fibrous plants and the electrochemical properties of final commodities containing activated carbon. This study's findings might be useful in developing high-performance activated carbon electrodes from a biomass carbon source. When compared to two other biomass materials, "*saussurea involucrata*" has a 2.5 times larger ionic diffusion coefficient than cotton stalk. This phenomenon demonstrates that the rate of ion transmission changes with pore shape.

According to research published in [16], an in-situ oxidative polymerization technique was used to create a MoSe₂-Polyaniline (PANI) nanocomposite with various amounts of MoSe₂ (0.05 g, 0.1 g, and 0.2 g). The form and weight

percentage ratio of nanocomposites (FESEM) were investigated using field emission scanning electron microscopy and energy dispersive X-ray spectroscopy (EDX). X-ray Photoelectron Spectroscopy (XPS) measurements of the nanocomposite's atomic and weight concentrations produced results that agreed with those of the EDX investigation. The best nanocomposite for a supercapacitor electrode material achieved a maximum specific capacitance of 463 F/g at a scan rate of 5 mV/s and retains around 72% of that specific capacitance after 3000 charge-discharge cycles. The MoSe₂-PANI nanocomposite has an energy density of 19.6 Wh/kg and a power density of 12.7 W/kg. The electrochemical activity of the MoSe₂-PANI electrode was increased by combining the advantages of electrical double-layer capacitors (MoSe₂ nanosheets) and pseudo-capacitors (Polyaniline nanofiber). The MoSe₂-PANI nanocomposite increased the wettability of the electrode material as well as the electron and ion transport pathways. The thermogravimetric analysis (TGA) of the nanocomposite revealed that it had increased thermal stability with a mass loss of just 28%. The Brunauer-Emmett-Teller (BET) analysis verifies the large surface area (61.147 m² g⁻¹) and pore volume as compared to their virgin samples (8.595 cm³ g⁻¹). Because of its outstanding electrochemical performance, MoSe₂-PANI nanocomposite has enormous potential for use as an electrode material in energy storage devices.

Gel-based electrolytes are gaining popularity as an important component of this system because next-generation green wearable and flexible energy storage devices are needed, but present materials are troublesome due to poor performance. This is the case, as shown by optimization specialists' findings in [17]. The substance's value must be preserved by allowing it to be twisted into amorphous gels, which are easy to manufacture in large quantities without

the toxic chemical binders used in everyday life. An example of a breakthrough storage system driven by an electrolyte built of genetic DNA is discussed. The DNA gel is amorphous and has a strong electric field. The device possesses strong ionic conductivity, mechanical integrity, and a higher maximum specific capacitance to liquid and other gel electrolytes. In LED lighting, the more flexible DNA gel supercapacitor (D-gel-SC) provides the maximum energy and power density. Even poor environmental conditions will not impact performance further. This material has the potential to be used in advanced energy storage systems.

According to study by supercapacitor design specialists in [18], supercapacitors (SCs), a breakthrough kind of green electrochemical energy storage device with excellent power density and long-term durability, have a significant potential to replace non-renewable energy sources. Because of their economic and environmental advantages, aqueous SCs have enormous promise in a variety of industries. However, the relatively small voltage window of aqueous SCs inhibits future development. There has been a lot of progress reported in aqueous SCs with ultrahigh voltage windows (>2.0 V) in the recent several years, notably in the last five. The effects of theoretical processes on the voltage window are first studied. These are the primary processes for broadening the voltage window of aqueous SCs. Following that, the techniques for producing aqueous SCs above 2.0 V are thoroughly reviewed and classified into three categories: electrode modification via structural engineering, metal cation doping and advanced composite fabrication, and electrolyte optimization via the development of "Water in Salt" and novel mixed electrolytes. Finally, various future research avenues for these >2.0 V aqueous SCs (ASC) are proposed based on current advancements and deficiencies.

Work in [19] discusses the study of high-density supercapacitor devices. Electronic components used in energy harvesters must be mechanically conformable in order to maximize user comfort. researchers demonstrate that laser-induced graphene may be used to make flexible, inexpensive, and effective graphene supercapacitor electrodes (LIG). A CO₂ laser beam instantly transforms the poly-ether-sulfone polymer (PES) into a highly porous carbon structure. To make the electrodes for the supercapacitor, graphene layers were deposited on graphite sheets using the LIG technique. Among the techniques used to examine and validate graphene production and shape were scanning electron microscopy (SEM), energy dispersive X-ray (EDX) spectroscopy, Raman spectroscopy, and Fourier transform infrared spectroscopy. In addition, electrochemical characterization in a variety of various electrolytes was carried out (NaOH and KOH). At 5 mV s⁻¹, the LIG electrode produced 165 mF cm⁻² and 250 mF cm⁻² in NaOH and KOH electrolytes, respectively. In light of this, researchers show that a symmetric, wearable supercapacitor with LIG electrodes can generate 98.5 mF cm⁻² in KOH electrolyte at 5 mV s⁻¹. At 0.5 mA cm⁻², the device has an energy density of 11.3 Wh.cm⁻² and a power density of 0.33 mWcm⁻². It is unusual for electrodes made of similar graphene to survive 2000 cycles with 75% of the capacitance intact. These findings support the use of LIG in the development of adaptable energy harvesters for wearable technology.

Work in [20] investigates the design and laboratory implementation of a full-scale physical simulator of an all-silicon carbide (SiC) traction motor drive for light-rail transit systems (LRTS) with an onboard supercapacitor energy storage system. (ESS). The device consists of a three-phase two-level PWM traction inverter that powers a three-phase squirrel-cage traction motor, a flywheel

attached to the motor shaft that simulates the vehicle's dynamic behavior, a loading generator connected to the grid via a dc-link converter with active front-end, and a supercapacitor ESS. The PWM rectifier, which represents the 750 V dc catenary line, also serves as a system model. The PWM rectifier, traction inverter, and bidirectional dc-dc converter are three SiC power MOSFET-based converters with high efficiency and power density. A physical simulator is useful for all SiC converter design and testing. It can evaluate the performance of various control, modulation, and energy-saving techniques and comes with software packages for a catenary model, rail track model, and vehicle model. This study's physical simulator system also allows for real-time benefits assessment of the onboard supercapacitor ESS as well as performance testing of a vehicle formation on a predetermined track under various use cases.

According to research by supercapacitor optimization experts in [21], the industry for smart consumer electronics is poised to skyrocket. Textile-based electronics are gaining prominence. Flexible and wearable electronics research, which might serve as power sources for wearable devices, is now brisk. A flexible yarn-based supercapacitor (YSC) for flexible/wearable energy storage applications is developed utilizing TiO₂ nanofibers and multiwalled carbon nanotubes synthesized on carbon yarn through a simple electrophoretic deposition technique. The active chemicals on carbon yarn are compressed, physically strong, and unbound, which facilitates charge/ionic transmission. The capacitance of the built-in YSC device is 36.8 mF/cm at 0.1 mA/cm current flow. Furthermore, even after 10,000 cycles, the device maintains 90% of its capacitance, demonstrating exceptional mechanical stability for energy storage. The YSC's great degree of flexibility is shown further by the fact that it retains 95% of its

original shape after 2000 cycles of bending at 0.5 mA/cm. With a maximum energy density of 11.5 Wh/cm and a power density of 368 W/cm, the YSC device beats several YSCs reported in the literature. Three YSCs integrated in a wearable fabric flash a red LED for more than five minutes in the movie to demonstrate its use.

To mention a few essential aspects and factors, the fabrication of the electrode and electrolyte, the building of the cell, and the packaging are all critical to the design and construction of an all-solid-state supercapacitor (SC) energy storage device. This is based on studies offered by optimization specialists in [22]. The goal of our study is to develop an all-solid-state supercapacitor employing flexible PVA/TiO₂ nanocomposite polymer electrolyte membranes (NCPiEMs) as electrolyte cum separators and multi-walled carbon nanotubes (MWCNTs) as electrodes. Out of all the TiO₂ nanofiller and PVA polymer combinations tested, the combination of 3wt TiO₂ provided the maximum energy storage capacity in a two-electrode arrangement. The mechanical stability (up to 50.21 MPa), thermal stability (up to 280 °C), and electrochemical performance of PVA/3wt TiO₂ mix membranes were exceptional. The improved ionic transport at the electrode-electrolyte interface enabled the SC to attain a specific capacitance of 137.72 F/g and an energy density of 19.12 Wh/Kg. There was also a great power density of 277.7 mW/Kg at 1 A/g and a good capacitance retention of 94.08% after 6000 cycles. This idea was validated by studies comparing the electrochemical performance of the PVA/3wt%TiO₂ membrane to the commercially available Nafion 112 membrane employing comparable MWCNT electrodes.

Although integrated systems need a constant working voltage to function, this requirement has been hurt by abrupt high-power demands

and the resulting voltage disturbance, according to a study published in [23] by specialists in supercapacitor design. To fulfil power needs and keep the system running, an on-chip micro supercapacitor (MSC) with a high capacitance density might be used as a viable high-power supply unit. The MSC's considerable capacitance decay, however, drastically decreases the device's power output at high charge/discharge rates, making it worthless. This work demonstrates an on-chip high-power MSC with increased capacitance density, fast charge/discharge speed, and scaling-down capability. The inclusion of mesoporous gold in the electrode framework provides a rapid electronic/ionic channel while limiting porous effects at high charge/discharge rates. A homogenous MnO₂ active layer with a high pseudo-capacitance that is generated via an electrochemical potential-modulated deposition technique also contributes to the improvement. Furthermore, the asymmetric electrode configuration tries to enhance the voltage needed for single device operation. Because of the high stable capacitance density of 9 mF/cm² and the low-capacity loss of 28% at the quick scan rate of 1 V/s, an unprecedented power density of 138 mW/cm² was obtained.

High-density supercapacitor inventors provide a wind-solar hybrid power system (WSHPS) dispatching approach for a one-hour dispatching period for a full day in [24], using a battery and supercapacitor hybrid energy storage subsystem. (HESS). A frequency management mechanism is employed in the HESS design to extend battery life by aggressively using both the high energy density of batteries and the high-power density of supercapacitors. A low-pass filter (LPF) separates power between a battery and a supercapacitor (SC). The cost optimization of the HESS based on the LPF's time constant is calculated using extensive simulations on the MATLAB/SIMULINK platform. The curve fitting and particle swarm

optimization methodologies are used to get the optimal LPF time constant value. A variety of control algorithms are developed as functions of battery state of charge to achieve precise grid reference power computation for each hour of dispatching. This computation guarantees that the HESS has adequate capacity to operate the next day while also lowering the cost of energy storage. Cycling and calendar costs, as well as the most cost-effective energy storage cost for hourly dispatching WSHPS electricity, are considered for establishing the correct depth of discharge for HESS. This research also includes a cost-benefit analysis of several energy storage solutions for WSHPS hourly dispatching. The simulation results show that the suggested HESS outperforms battery- or SC-only operation.

In their work [25], researchers that specialize in supercapacitor optimization proposed employing graphene oxide (GrO) as the electrode material. GO was created using natural graphite precursors with varying flake sizes. GO was examined using Elemental Analysis (EA), High-Resolution Transmission Electron Microscopy (HRTEM), Fourier Transform Infrared (FTIR), and Raman spectroscopy. Cyclic voltammetry was used at different scan speeds to determine the exact capacitance and energy density of the electrode material. Specific capacitance increased as the size of the graphite precursor flake increased. At a scan rate of 10 mV/s/1, the GO sample, which was made from a precursor of graphite with an average particle size of 0.45 μm , had a specific capacitance and energy density of 204.22 F.g./kg and 102.11 kJ/kg, respectively. This sample also had the greatest specific capacitance across all scan rates.

This is mentioned by supercapacitor optimization experts in their work in [26]. Higher train densities on subway and tramway lines are a result of increasing urbanization,

population, and travel demand, which weakens the energy-feeding dc substations that power these alternative means of urban transportation. Because of voltage sags in the upstream ac grid, resistive voltage dips in dc feeders, and the constant power load (CPL) characteristic of subway and tramway traction units, such conditions may produce large fluctuations in the dc-link voltage. The work proposes a supercapacitor-based active stabilizer (SBAS) with a two-mode control method to solve this problem (TMCS). It is shown that the proposed SBAS acts in a suitable manner for shifting bus side capacitance. This feature, in conjunction with the suggested TMCS based on model predictive control (MPC), is used to improve system stability and eliminate dc-link voltage variations. To demonstrate the benefit of the proposed strategy, a simulation of a typical subway system and a series of experiments on a scaled-down prototype are employed. The results show that when the proposed SBAS is employed, the dc-link voltage loss never exceeds 2%. According to real-time hardware-in-the-loop (HIL) testing, the proposed MPC-based TMCS is likewise real-time practical.

According to study iterations provided by optimization experts in [27], researchers are attentively researching supercapacitor technology to cope with a reduction in battery power density. A hybrid battery-supercapacitor storage (HBSS) design that blends battery energy density with supercapacitor power density has been proven to improve overall efficiency. Despite significant study in the electric vehicle (EV) industry, the experimental use of this hybrid storage technology in the power grid to cope with the non-dispatchable nature of wind and solar energy is still in its early phases. This paper examines its practical use on a lab-scale hybrid microgrid at Southern Illinois University in Carbondale, Illinois, which employs two wind turbines and two solar (PV) modules. The program's purpose is to

encourage the electrical industry to employ lab-scale HBSS that has been scientifically validated.

The bulk of today's sensor nodes are powered by batteries; however, batteries have a limited lifetime, according to specialists in supercapacitor development [28]. Energy harvesting is used to extend the life of sensor nodes. This system uses or stores the energy collected by transducers such as thermoelectric generators based on environmental variables. This study looks at how to build a thermoelectric energy harvesting system using a supercapacitor and four different maximum power point tracking (MPPT) algorithms. The Perturb and Observe (PO), Incremental Conductance (INC), Open Circuit Voltage (OCV), and Short Circuit Current (SCC) algorithms were used to test the proposed circuit. Finally, the OCV algorithm was determined to be the fastest at charging the supercapacitor.

Work in [29] discusses the study of high-density supercapacitor devices. Currently, most energy storage systems employ passive balancing techniques, which require a long time to balance. By replacing a central dc-dc converter with a series of modular power converters, researchers were able to speed up the charging and balancing of a supercapacitor stack. A strategy for regulating power distribution (RPD) among the converters during the charging phase has been proposed to balance the supercapacitors. Certain converters, however, experience control saturation due to voltage differences across supercapacitors caused by their nonuniform conditions and characteristics. This article is noteworthy because it changes an energy-based technique to account for saturation in order to balance supercapacitors and correct power imbalances. Simulation and laboratory studies were used to

demonstrate the technique's advantages and disadvantages.

The supercapacitor, which is made up of several supercapacitor cells linked in series and is often used as a storage battery in practical applications, is examined in work published in [30] by supercapacitor optimization experts. To precisely anticipate the State of Charge (SoC) in the module, a comparable model of the supercapacitor cell module is employed. This model is anticipated to correctly describe the supercapacitor cell module's features, notably the standing self-discharge characteristics. The results of parameter identification have a direct influence on the validity of the model. Although the majority of supercapacitor equivalent models for supercapacitor cells have been proposed, defining the module equivalent model by connecting a number of supercapacitor equivalent models in series would result in additional and cumulative errors, affecting the model's accuracy and leading to parameter identification errors. The work develops a three-branch equivalent circuit model for the supercapacitor cell module in order to get exact identical model characteristics. The Recursive Least Squares Method (RLS) and the Circuit Analysis Method (CA) are then described in detail (RLS). This study develops a Simulink simulation model for the multi-method parameter identification of a supercapacitor cell module in order to highlight the advantages and disadvantages of CA and the Circuit Analysis-Recursive Least Squares Method (CA-RLS). Following that, it provides a segmentation optimization-based approach for determining the parameters of the similar circuit model for the supercapacitor cell module (SO). The results reveal that SO can more correctly reflect the supercapacitor cell module's charging and self-discharge properties. SO's utility is supported by both simulation and error analysis. In the static self-discharge phase, the comprehensive error is 0.28 percent, which is 6.83 percent and

0.64 percent lower than CA and CA-RLS, respectively.

In their study [31], experts in supercapacitor optimization presented the results of testing and modelling operations on large commercial supercapacitor cells at high current. Four commercial cells (FCC) with rated capacitances of 3000 F and rated voltages of 2.7 V are considered. While the current remains constant, all cells go through a series of charge/discharge cycles. The test current is set between 80 and 130 A, which is equal to the maximum operational current of the cells, which is 150 A under normal working circumstances. The cell circuit model is also constructed and validated against experimental data to ensure that it properly depicts the most significant dynamic behavior while keeping a good balance between the model's parameter complexity, simplicity, and robustness. It is shown that all of the commercial cells under examination have the same characteristics and circuit model. It is also shown that the circuit properties of the cells are comparable and that they have a shaky connection to the test current. Users get complete access to all of the circuit characteristics scrupulously recorded by the cells.

Optimization specialists present a simpler supercapacitor model and a parameter identification approach based on universal adaptive stabilization and optimization (UAS+O) in [32]. Analytical parameters for the current, voltage, and responsiveness of supercapacitors to cyclic voltage and current sources of varying amplitudes and frequency, which correspond to the driving cycles of electric autos, are reported. The presence of hysteresis in the I-V correlations of supercapacitors reveals simultaneous energy storage and dissipation. A simple comparable circuit model is provided to adequately represent hysteresis and I-V characteristics. The

proposed UAS+O-based technique for model parameter estimation is supported by simulations, experimental data, and mathematical arguments.

The study in [33] addresses the synthesis, characterization, and electrochemical analysis of composites consisting of copper nanoparticles grafted on graphitic carbon nitride for low-cost, high-performance supercapacitor applications. According to structural and morphological characterizations, in situ grafting of copper nanoparticles onto graphitic carbon sheets was effectively accomplished using a simple synthetic approach (SGC NGC). Many electrochemical investigations were conducted to determine how the proposed electrode material would work super-capacitively. In terms of electrochemical performance, the proposed nanocomposites outperformed pure graphitic carbon in these experiments. The equivalent series resistance of copper with graphitic carbon was calculated to be 1.61 based on the Nyquist plot of the EIS spectra, which is lower than the equivalent series resistance of graphitic carbon sheets used as the basis material. An asymmetric solid-state supercapacitor with a specific capacitance of 265.25 Fg/1 at 0.5 Ag/1 current density and an energy density of 36.87 Wh/kg at 2.50 kW/kg was produced. Furthermore, 5000 cycles at 5 Ag 1 with good cyclic consistency resulted in 79.4% capacitance retention. These electrochemical studies reveal that copper graphitic carbon nanocomposites have a high energy storage potential.

Researchers used a stochastic supercapacitor model [34] to estimate losses for different balancing schemes proposed by high-density supercapacitor designers. It also makes suggestions for developing supercapacitor banks with balancing networks. A supercapacitor may be the primary component of an energy storage system (ESS) that offers

high power to a DC or AC grid (SC). This is important in networks where renewable energy is widely used to maintain a balance between production and consumption. The cornerstone for the design technique is the supercapacitor model, which employs the stochastic variables capacitance, series resistance, and self-discharge current (SVC SR SDC). To comprehend how balancing networks, both dissipative and non-dissipative, affect the overall performance of the SC bank, when evaluating alternative strategies, the efficacy, cost, and complexity of the bank's balancing network are taken into account.

Wind shear and tower shadow effects, according to specialists in supercapacitor optimization, produce significant variations in wind turbine power production [35]. (WTs). As a consequence, in WT-integrated microgrids (MGs) with battery energy storage, these power fluctuations may cause battery micro-cycles, reducing battery life dramatically. The purpose of this work is to investigate how battery micro-cycles impact battery life and to suggest a solution for decreasing these micro-cycles in a wind-diesel microgrid utilizing a hybrid supercapacitor-battery energy storage device. The Discrete Fourier Transform (DFT) is utilized to separate the frequency components of the WT output power and determine the size of the supercapacitor in order to effectively reduce battery micro-cycles. The power converters' design, power distribution system, and control are all discussed. The software packages MATLAB/Simulink, TurbSim, AeroDyn, and FAST are used to correctly simulate the MG, wind shear, and tower shadow effects. Finally, two case studies that utilize either batteries alone or batteries in conjunction with supercapacitors are employed in simulation to assess and confirm the efficacy of the proposed strategy. There is also a cost-benefit analysis of the proposed system. According to the data, the proposed method

may efficiently minimize battery micro-cycles, hence increasing battery life and minimizing system costs.

According to research on supercapacitor optimization reported in [36], a Pinning-based Switching Control Model (PSCM) is employed to govern supercapacitor charging and cell balance. The cyber-physical system (CPS) design for the developed supercapacitor energy storage system consists of a physical layer, a cyber layer, and a control layer. In the physical layer, a switched resistor circuit is utilized to charge and balance supercapacitor cells, and switched system theory is employed to quantitatively explain the physical system. In the cyber layer, graph theory is employed to establish the accessibility of the reference voltage as well as the accessibility of information from surrounding cells. To balance cell voltages during charging, a switching control rule based on pinning is recommended for the control layer. The CPS's closed-loop model is built using a block diagram, and its stability is thoroughly evaluated. A testbed has been developed in a lab to validate that the recommended approach works. In-depth testing results reveal that the proposed pinning control technique, when compared to the present decentralized control strategy, may reduce voltage variance and boost energy efficiency. The practical challenges associated with implementing the recommended strategy are also addressed.

According to the study of optimization experts in [37], the constant-current constant-voltage (CC-CV) charging strategy is a common approach for charging many batteries at once. As a consequence of the recent development of high power-density batteries, such as supercapacitors, several chargers are often coupled in parallel to provide the required charging power in a variety of applications. However, the present imbalance caused by the

old decentralized control technique jeopardizes the reliability of the multi-charger system. In this work, the CC-CV charging protocol is extended to multi-charger systems (CCCV MCS) by using a cooperative control mechanism that effectively eliminates charger current imbalance. The reason for this study, as well as the charging system modelling, are first discussed. Then, depending on the voltage of the supercapacitor, a switching logic is built to switch between a cooperative CC charging protocol and a cooperative CV charging protocol. The block diagram is used to define the closed-loop idea of the proposed charging system. The effectiveness of the proposed technique is evaluated in a laboratory environment. According to experiment results, the proposed approach outperforms existing decentralized control techniques in terms of current balance and voltage regulation.

According to research by professionals in the supercapacitor design sector documented in [38], supercapacitor energy storage systems (ESS) are often used in subways to absorb the regenerative braking energy of trains. Even when roadside ESS is used often, the brake resistor remains engaged owing to the impacts of no-load voltage and other reasons. Because the auxiliary ESS cannot collect all of the regenerative braking energy, energy is squandered. In this study, the on-board brake resistor is completely replaced by a specialized on-board super-capacitor, and a hierarchical optimization energy management approach based on a DC-side series super-capacitor design is also proposed (EMS). The EMS is divided into three levels: To begin, by using the inverter and motor's short-term overvoltage capability, the system may boost the inverter-side voltage in a short period of time without affecting the voltage of the traction network, therefore improving the train braking characteristic curve. Even under extreme conditions, a roadside supercapacitor can be

managed in sync with remaining regenerative braking energy. Finally, this technology may effectively minimize system loss by adjusting the DC voltage on the inverter side based on loss calculation and current prediction. The proposed control strategy is examined using the RT-LAB experiment, and the findings support the hypothesis.

High-density supercapacitor designers offered a paradigm for improving power distribution between a battery and supercapacitor in an electric vehicle energy storage system in [39]. A convex optimal control formulation is proposed, which reduces overall energy consumption while imposing severe limitations on power output and total energy stored in the battery and supercapacitor. The ADMM technique is suggested, since its computational and memory requirements rise linearly with the size of the prediction horizon (and can be reduced using parallel processing). When compared to a low-pass filter against an all-battery baseline, numerical simulations reveal that the best controller greatly reduces battery deterioration. This is shown by reductions in peak battery power of 71.4%, root-mean-squared battery power of 21.0%, battery throughput of 13.7%, and energy consumption of 5.7%. Furthermore, it has been shown that the ADMM technique, a feasible replacement for online receding-horizon control, can solve the optimization problem fast and effectively for prediction horizons bigger than 15 minutes.

The study of supercapacitor optimization experts [40] investigates how the regenerative braking system based on supercapacitors enhances the motor's energy use efficiency. The supercapacitor, on the other hand, would lose energy from the power grid as a consequence of a power imbalance between the energy storage unit and the motor. This study proposes a multi-parameter collaborative power prediction control of the motor-driven system to overcome

the power mismatch. The energy flow process is being studied. The model for supercapacitor power prediction is then created utilizing a variety of signals in certain time frames. Modelling is done using discrete forms, and interactions between distinct components (IDC) are taken into consideration. The performance optimization function considers the notion of using the least amount of energy. The energy of the supercapacitor, the energy of the power grid, and the power of the motor may all be completely coordinated to maintain the dynamic supply-demand power balance. Simulation and experimental results are utilized to support the effectiveness of the proposed control approach. The proposed operating condition consumes 20% less energy than the standard control technique settings.

This is investigated by supercapacitor optimization experts in [41]. This article proposes a global optimal operation and control solution based on the fuel cell/supercapacitor hybrid tram in each segment between stations to reduce fixed line operation and maintenance expenses for the tram. This approach combines the hybrid system control method with a speed optimization strategy based on using the least amount of hydrogen and the least amount of energy. For the speed optimization method based on the energy consumption function of the tram in each section, the speed curve can be obtained; for the hybrid system control method based on the energy distribution of the tram in each section as well as the hydrogen consumption function of the fuel cell system (FCS), the speed curve According to real-world testing, the proposed approach can perform online tram control and has a significant influence on hydrogen consumption and FCS output fluctuation, which is, of course, the last but not least step.

According to studies presented by optimization experts in [42], the stationary supercapacitor

energy storage system (SCESS) is one of the most successful systems for harnessing train regenerative braking energy in urban rail networks. This research thoroughly examines train operating diagrams, substation no-load voltage, onboard brake resistor control, and SCESS capacity configuration. The equivalent circuit model is used to demonstrate the connections between train operating parameters and system energy consumptions, as well as the effects of traction power system features on energy transfer between powering trains, braking trains, and SCESSs. It is proposed to use a multi-variable synthetic optimization technique to concurrently optimize the SCESS capacity, train operating diagrams, and traction power system attributes. The design variables and control variables are repeatedly improved using a hierarchical multi-objective optimization model to reduce the search space and maximize the efficacy of the optimization process. Because traffic density has a considerable impact on how the system distributes regenerative braking energy, the optimization target function fully considers the frequency distribution of headways throughout the day. By merging the Elitist Non-dominated Sorting Genetic Algorithm (NSGA-II) with the traction power flow simulator, the flowchart for the two-stage optimization method and the pareto set for the multi-objective problem are generated. Case studies from the Beijing Batong Line demonstrate the advantages of the proposed algorithm's decreased setup and energy costs.

Work in [43] describes the work of supercapacitor design professionals. Energy storage devices are a technical barrier to the development of environmentally friendly automobiles. Automobile manufacturers are attempting to develop battery technology and forecast how it would respond in this circumstance. This paper proposes an improved electrothermal modelling analysis of a hybrid

energy storage system comprised of lithium-ion batteries and supercapacitors. The purpose is to make it feasible to account for the ages of the system's components. A model that integrates electrothermal properties may be used to analyze the performance deterioration of the hybrid energy storage system. A hybrid particle swarm-Nelder-Mead (PSO-NM) optimization approach defines the two components of the hybrid system using experimental data from an urban electric car. The results illustrate the efficacy of the developed model and testify to the feasibility of our method. Because the observed inaccuracy is less than 3%, the use of the PSO-NM optimization strategy considerably boosted the efficacy of parameter identification for the generated model. In many cases, combining an updated model with an updated size approach allows you to evaluate energy management techniques in applications for electric vehicles.

According to studies presented by high-density supercapacitor designers in [44], energy storage technologies such as batteries and supercapacitors are gaining traction in a number of industrial applications because they provide higher dynamic responsiveness and efficiency. Electric versions of batteries and supercapacitors must be accessible in this condition for successful power system design, operation, and energy management. In order to identify the features of the appropriate electric model, the identification current profile often occurs as a charge or discharge pulse. These models are then validated using the most current verification profile. Because the verification profile is more dynamic in amplitude and frequency than the identification profile, the identification signal's confined bandwidth causes validation errors. This study proposes a different Pulse - Pseudo Random Binary Sequence (PP RBS) identification current profile with equivalent spectral features to the verification profile in order to improve

modelling accuracy. To calculate the attributes of a lithium-ion battery and a supercapacitor, utilize the Optimization Toolbox in Matlab and electrical models in Simulink or Simscape. For electric vehicle applications, the models are verified using the Urban Driving Cycle ECE-15 and the Hybrid Pulse Power Characterization (HPPC).

Work in [45] describes the studies of supercapacitor optimization experts and explores The high cost of energy storages, such as batteries, which are necessary owing to the intermittent nature of diverse energy sources, often inhibits renewable energy sources from being commercialized. Because of their low average power densities and limited cycle lifetimes, batteries are becoming increasingly expensive to replace. Several applications have shown the capabilities of a battery supercapacitor-hybrid energy storage system (BS-HESS) with an efficient energy management system (EMS) to extend battery life. Using the Pontryagin's Minimum Principle (PMP), researchers suggest the optimal power distribution between a supercapacitor and a battery in a HESS for a freestanding solar-aided agricultural feed mill, therefore improving battery life under real-time use cases. To account for the effects of partial shadow and to respond quickly to unexpected changes in sun irradiation, researchers use a specific technique known as hybrid maximum power point tracking, which entails adding an extra term to the performance index. researchers validate the effectiveness of the proposed PMP-based EMS by modelling it and comparing it to known approaches. According to simulation results, merging HESS with PMP-based EMS may boost battery cycle life when compared to rule-based EMS and battery-only storage. Finally, researchers implement the proposed PMP-based EMS in a hardware prototype to illustrate its practicality. The results were positive.

According to [46], supercapacitor optimization experts should create a supercapacitor that is both environmentally friendly and has great electrochemical performance. One new endeavor in the literature to lessen the environmental effect of supercapacitors is the substitution of efficient but toxic organic electrolytes with safe, biocompatible ones, such as a sodium salt solution and a hydrogel. Because these bio-friendly electrolytes do not function as well as toxic organic electrolytes, they have not been shown to be a viable substitute. The findings reveal that a novel approach for integrating carbon nanotubes (CNTs) into a sodium salt hydrogel-based electrolyte (NaH) may significantly increase its capacitance. As a result, in terms of energy and power densities in the supercapacitor, the CNT-loaded bio-friendly electrolyte beat both a CNT-free electrolyte and a hazardous organic electrolyte based on DMSO.

According to a study published in [47], supercapacitors are attracting significant interest in wireless sensor network applications due to their high-power density and longer lifespan. The influence of leakage must be considered in the online control and management of supercapacitors in these applications. As a consequence, researchers provide in this paper an online approach for determining the state-of-charge (SOC) of supercapacitors while accounting for leakage. First, researchers provide an observable equivalent circuit model (ECM) of a supercapacitor that includes the leakage effect. Based on the recommended ECM, researchers next compute an unscented Kalman-filter-based (KF) SOC estimate. researchers demonstrate the proposed system and conduct experimental testing to identify the ECM parameters using a commercially available supercapacitor (Maxwell BCAP0005). In this paper, researchers also do simulations and tests to assess the efficacy of the proposed estimation approach. The resilience of the

proposed system to parametric and measurement error is then evaluated.

According to research by supercapacitor design specialists in [48], micro supercapacitors (MSCs) with ultrahigh capacitance densities and thin-film fabrication capabilities are appealing energy storage and power-filtering devices for integrated systems. However, wafer-scale manufacture and encapsulation of MSCs are problematic owing to the incompatibility of chemically active electrolytes with traditional microfabrication processes. researchers explain in detail the novel electrolyte deposition and device packaging processes employed in the wafer-scale manufacturing of well-encapsulated MSCs. Because the proposed encapsulating approach only impacts the spin-coating and photolithography processes, it is low-cost, high-throughput, and naturally scalable. According to the findings of the experiments, the encapsulation method (EM) extends device longevity while having no effect on capacitive performance. The prototype MSC meets the criteria for AC-line filtering by having a capacitance density of more than 2 mF/cm² at a quick scan rate of 10 V/s and an 8 ms time constant. Process consistency, operating leakage current, and temperature endurance range were also investigated and addressed. This research will significantly enhance the way MSCs are employed in real applications.

According to the research of high-density supercapacitor designers reported in [49], tin selenide (SnSe) has been investigated as one of the primary binary IV-VI compounds for a variety of energy storage applications in the class typical layered metal chalcogenide family. The two-dimensional hexagonal tin selenide nanosheets were created using a one-pot colloidal technique and then tested as the active electrode for supercapacitors. The as-prepared SnSe electrode has a capacitance of 617.9 F/g at a scan rate of 2 mV/s and excellent

electrochemical stability due to effective ion transport from the electrolyte to the active electrode and charge transport from the electrode to the current collector. Because of the morphology-aided electrochemical activity, the electrode exhibits a high energy density of 28.5 Wh/kg and excellent cycle stability. The findings indicate that the simple synthesis process proposed for manufacturing binder-free electrodes has a promising future in the development of high-performance energy storage devices.

According to research presented by supercapacitor optimization specialists in [50], bio-wastes are a fantastic source of carbon with exceptional electrical conductivity and a large specific surface area for non-faradic charge adsorption. Metal oxides, on the other hand, have the capacity to store charges in a faradic manner due to their intense redox activity. researchers use activated carbon (NDAC) derived from UiO-66 and zirconium oxide-based electrodes derived from neem leaves (*Azadirachta Indica*) in this study. The NDAC has a high specific capacitance of 262 F/g at 1 A/g when used as the negative electrode in a three-electrode system with sodium sulphide as the electrolyte. When the same electrolyte was used, the positive electrode material ZO produced a high specific capacitance of 337 F/g at a current density of 0.25 A/g. An asymmetrical supercapacitor is also built with sodium sulphate electrolytes, charged balanced NDAC, and ZO electrodes. The asymmetrical NDAC/ZO-based device has a 78% cycle life and a maximum energy density of 49.2 Wh/kg at a high-power density of 540 W/kg. These findings open up new possibilities for developing next-generation high-energy density hybrid supercapacitors based on low-cost biowaste and metal oxides derived from MOFs. Thus, it can be observed that a wide variety of models are proposed by researchers for improving density of super-capacitors. To

further analyze these models, next section of this text compares them in terms of efficiency, scalability, operational speed, deployment cost and complexity levels. Which will assist readers to identify optimal models for their real-time use cases.

3. Result analysis & comparison

After conducting a comprehensive analysis of the existing density optimization models for supercapacitors, it has been discovered that the majority of these models employ electrolytic fusions, while others use some combination of modeling techniques. This was discovered as a result of the extensive review that was conducted. This part compares the models that have been assessed in terms of their efficiencies, scalability, operational speed, cost of deployment, and complexity levels. The goal of this section is to make the model selection process even simpler. The efficiency (E), is measured in terms of the performance of optimizing the density, and the operational speed (D), is measured by measuring the amount of time required to charge and discharge these capacitors. The cost of deployment (abbreviated as DC), as well as the complexity of deployment (abbreviated as C), is calculated in terms of the overall cost required to deploy these models as well as the complexity of the models' internal deployment. While the Scalability (S) is calculated in terms of the number of applications for which the model can be deployed under normal operating circumstances. All these parameters were quantized into Low Value Quantization (LVQ), Medium Value Quantization (MVQ), High Value Quantization (HVQ), & Very High Value Quantization (VHVQ), and their performance was tabulated in table 1 as follows,

Model	C	D	DC	E	S
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MDT [1]	H	M	VH	M	VH
GPA [2]	H	H	H	M	H
RLS KF [3]	M	H	H	H	H
TiO2 MnO2 [4]	H	M	VH	M	VH
Fuzzy SRPC [5]	M	L	M	H	H
MANF [6]	H	H	H	M	H
NCMP [7]	H	M	H	M	H
MSC [8]	VH	H	VH	H	H
DFT [9]	VH	M	H	M	VH
MOF [10]	H	M	H	H	M
ZI HSC [11]	H	H	VH	M	M
ASA PPY [12]	VH	M	H	M	VH
VMOF [13]	L	L	L	VH	VH

MOS2 [14]	H	H	H	H	H
HO MAC [15]	H	H	VH	H	H
MoSe PANI [16]	L	L	M	VH	VH
DNA [17]	M	M	H	H	H
ASC [18]	H	H	VH	M	M
LIG PES [19]	M	M	VH	H	H
LRTS [20]	H	H	H	H	VH
TiO2 YSC [21]	H	H	VH	M	H
NC PEM MW CNT [22]	M	M	H	H	L
MnO2 MSC [23]	H	H	VH	M	H
LPF [24]	M	H	H	M	H

GrO [25]	M	H	H	H	VH
SBAS [26]	H	VH	H	M	H
OCV [28]	H	H	VH	H	M
RPD [29]	H	H	M	H	M
RLS CA [30]	VH	M	H	M	H
FCC [31]	H	H	VH	M	H
UASO [32]	H	H	H	H	VH
SGC NGC [33]	M	H	M	H	H
SVC SR SDC [34]	H	M	H	M	H
DFT [35]	H	M	VH	H	L
PSCM [36]	H	H	M	H	M
CCCV MCS [37]	VH	H	M	H	M

EMS [39]	H	H	VH	M	H
ADMM [40]	H	VH	H	M	H
IDC [41]	M	H	M	H	H
NSGA [42]	L	M	M	H	VH
PSO NM [43]	M	H	H	M	H
PP RBS [44]	H	H	H	M	M
PMP [45]	H	M	VH	M	L
CNT NaH [46]	H	H	H	H	H
KF [47]	H	VH	M	H	L
EM [48]	H	H	H	M	M
SnSe [49]	H	H	H	M	H
NDAC [50]	H	H	VH	H	M

Table 1. Performance estimation of density optimization models for supercapacitors

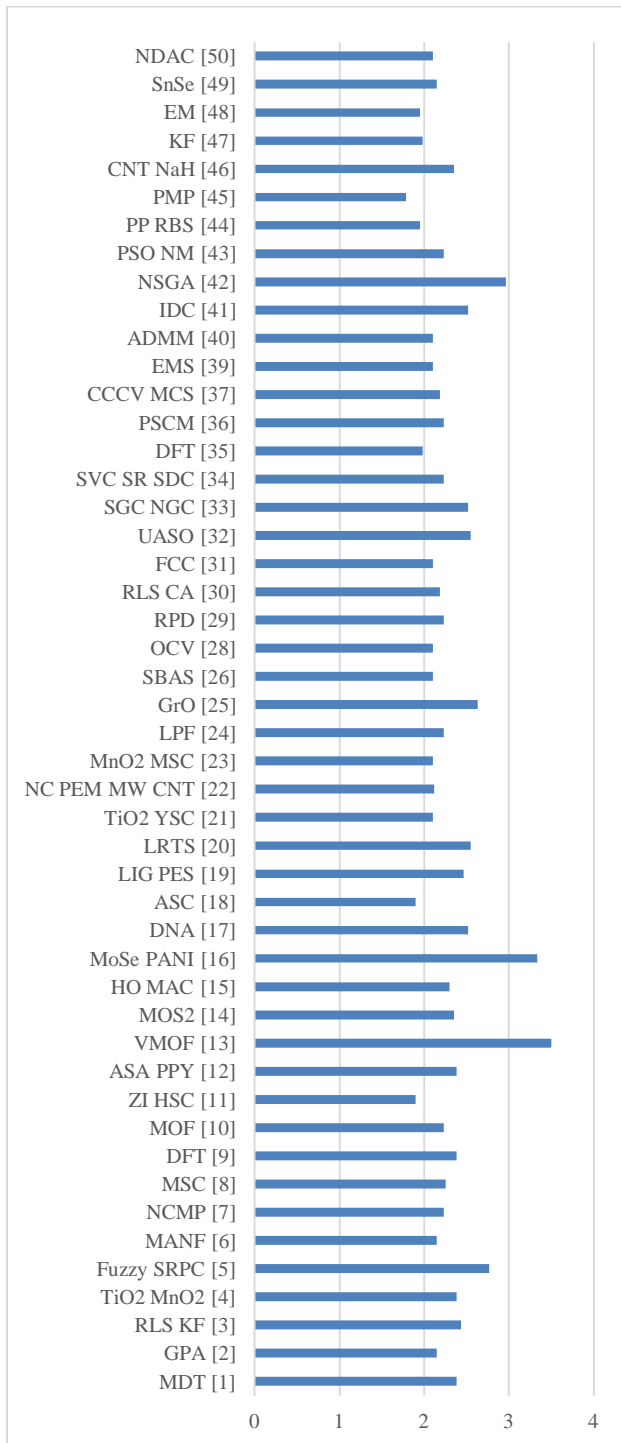


Figure 1. SCORM Performance for different models

Based on this analysis it can be observed that VMOF [13], MoSe PANI [16], and NSGA [42] are able to achieve low complexity, while Fuzzy SRPC [5], VMOF [13], and MoSe PANI [16] showcase low delay of operation, thus can be used for general purpose use cases.

Similarly, VMOF [13], Fuzzy SRPC [5], MoSe PANI [16], RPD [29], SGC NGC [33], PSCM [36], CCCV MCS [37], IDC [41], NSGA [42], and KF [47] are able to achieve lower deployment cost, while MDT [1], TiO₂ MnO₂ [4], DFT [9], ASA PPY [12], VMOF [13], MoSe PANI [16], LRTS [20], GrO [25], UASO [32], and NSGA [42] showcase higher scalability levels, thus can be used for large-scale scenarios.

In terms of efficiency of operation, VMOF [13], and MoSe PANI [16] are able to improve super capacitor performance, thus can be used for real-time deployments. All these metrics were combined to form a novel Super Capacity Optimization Rank Metric (SCORM), which is estimated as per equation 1,

$$SCORM = \frac{S + E}{5} + \frac{1}{D} + \frac{1}{DC} + \frac{1}{C} \dots (1)$$

As per this analysis and figure 1, it was observed that VMOF [13], MoSe PANI [16], NSGA [42], Fuzzy SRPC [5], GrO [25], LRTS [20], and UASO [32] showcase high efficiency in terms of delay, deployment cost, complexity, scalability and efficiency of operation, thus they must be used for practical deployment scenarios.

4. Conclusion & Future work

After conducting a thorough investigation into the existing models for density optimization of supercapacitors, it was found that the majority of these models use electrolytic fusions, while others use some combination of modeling techniques. This was discovered as a result of an exhaustive study of these models. The comprehensive review that was carried out yielded this finding as a consequence of its findings. Based on the analysis of these models, it was found that VMOF, MoSe PANI, and NSGA are able to achieve low complexity, while Fuzzy SRPC, VMOF, and MoSe PANI

showcase low delay of operation, and as a result, can be used for general purpose use cases. NSGA is the only one of these models that can achieve low delay of operation. In a similar fashion, VMOF, Fuzzy SRPC, MoSe PANI, RPD, SGC NGC, PSCM, CCCV MCS, IDC, NSGA, and KF are able to achieve reduced deployment costs. On the other hand, MDT, TiO MnO, DFT, ASA PPY, VMOF, MoSe PANI, LRTS, GrO, UASO, and NSGA display greater scalability levels

Both VMOF and MoSe PANI are able to increase super capacitor performance, and as a result, they are suitable for use in real-time deployments. This is due to their high efficiency of operation. After combining all of these metrics, it was discovered that VMOF, MoSe PANI, NSGA, Fuzzy SRPC, GrO, LRTS, and UASO showcase high efficiency in terms of delay, deployment cost, complexity, scalability, and efficiency of operation. As a result, these algorithms ought to be utilized for practical deployment scenarios. In the future, these approaches will need to be verified for large-scale scenarios. They also have the potential to be enhanced via material validations and the use of bioinspired models for the estimate of component ratings for real-time deployments.

5. References

- [1] Zhenxiao Yi, Kun Zhao, Jianrui Sun, Licheng Wang, Kai Wang, Yongzhi Ma, "Prediction of the Remaining Useful Life of Supercapacitors", *Mathematical Problems in Engineering*, vol. 2022, Article ID 7620382, 8 pages, 2022. <https://doi.org/10.1155/2022/7620382>
- [2] Senthil Kumar Kandasamy, S. Maheswaran, K. R. Kavitha, D. Karthikeyan, J. Indra, K. Sheikdavood, Y. Syamala, K. Srilakshmi, Chandrasekaran Arumugam, Dhivya Balamoorthy, "High-Performance Graphene Oxide/Polypyrrole/Ziziphus jujuba/Prunus dulcis Ternary Composite Electrodes for Supercapacitor for Sensor Applications", *Journal of Nanomaterials*, vol. 2022, Article ID 9201910, 10 pages, 2022. <https://doi.org/10.1155/2022/9201910>
- [3] Kai Wang, Chunli Liu, Jianrui Sun, Kun Zhao, Licheng Wang, Jinyan Song, Chongxiong Duan, Liwei Li, "State of Charge Estimation of Composite Energy Storage Systems with Supercapacitors and Lithium Batteries", *Complexity*, vol. 2021, Article ID 8816250, 15 pages, 2021. <https://doi.org/10.1155/2021/8816250>
- [4] Li Zhang, Qiong Song, Chunyan Wang, Xianjun Liu, Xiujuan Jiang, Jian Gong, "The Electrode Materials of Supercapacitor Based on TiO₂ Nanorod/MnO₂ Ultrathin Nanosheet Core/Shell Arrays", *Journal of Nanomaterials*, vol. 2020, Article ID 6642236, 11 pages, 2020. <https://doi.org/10.1155/2020/6642236>
- [5] Rui Zhu, An-lei Zhao, Guang-chao Wang, Xin Xia, Yaopan Yang, "An Energy Storage Performance Improvement Model for Grid-Connected Wind-Solar Hybrid Energy Storage System", *Computational Intelligence and Neuroscience*, vol. 2020, Article ID 8887227, 10 pages, 2020. <https://doi.org/10.1155/2020/8887227>
- [6] Tang, P., Zhao, Y., Xu, C. *et al.* Enhanced energy density of asymmetric supercapacitors via optimizing negative electrode material and mass ratio of negative/positive electrodes. *J Solid State Electrochem* **17**, 1701–1710 (2013). <https://doi.org/10.1007/s10008-013-2021-7>
- [7] Zong, Q., Tao, D., Yang, H. *et al.* Optimizing nanostructure and constructing heterostructure via Mo/W incorporation to improve electrochemical properties of NiCoP for hybrid supercapacitors. *Sci. China Mater.* **65**, 1195–1206 (2022). <https://doi.org/10.1007/s40843-021-1904-x>

- [8] Hepel, M.. *Electrochem Sci Adv* 2022, 00, e2100222. <https://doi.org/10.1002/elsa.202100222>
- [9] Zhang, H., Wang, L., Xing, X., Zhao, S., Wang, K., Liu, S. F., High-Energy-Density Supercapacitors Based on High-Areal-Specific-Capacity $Ti_3C_2T_x$ and a Redox-Active Organic-Molecule Hybrid Electrode. *Adv. Funct. Mater.* 2022, 2208403. <https://doi.org/10.1002/adfm.202208403>
- [10] Yaqoob, L, Noor, T, Iqbal, N. An overview of supercapacitors electrode materials based on metal organic frameworks and future perspectives. *Int J Energy Res.* 2022; 46(4): 3939- 3982. doi:[10.1002/er.7491](https://doi.org/10.1002/er.7491)
- [11] X. Gong, J. Chen, P. S. Lee, *Batteries & Supercaps* 2021, 4, 1529.
- [12] Yazar, S, Arvas, MB, Sahin, Y. An ultrahigh-energy density and wide potential window aqueous electrolyte supercapacitor built by polypyrrole/aniline 2-sulfonic acid modified carbon felt electrode. *Int J Energy Res.* 2022; 46(6): 8042- 8060. doi:[10.1002/er.7706](https://doi.org/10.1002/er.7706)
- [13] Li, Y., et al.: Preparation of metal-organic frameworks and their derivatives for supercapacitors. *Biosurf. Biotribol.* 8(3), 151–164 (2022). <https://doi.org/10.1049/bsb2.12040>
- [14] R. R., A. T. Prasannakumar, R. R. Mohan, M. V., S. J. Varma, *ChemistrySelect* 2022, 7, e202203068.
- [15] X. Zhang, Z. Li, X. Tian, Y. Ma, L. Ma, *ChemistrySelect* 2021, 6, 13015.
- [16] H. Mittal, A. Kumar, M. Khanuja, *ChemistrySelect* 2022, 7, e202201623.
- [17] Mitta, S. B., Harpalsinh, R., Kim, J., Park, H. S., Um, S. H., Flexible Supercapacitor with a Pure DNA Gel Electrolyte. *Adv. Mater. Interfaces* 2022, 9, 2200133. <https://doi.org/10.1002/admi.202200133>
- [18] Liu, J., Huang, Z. and Ma, T. (2020), Aqueous Supercapacitor with Ultrahigh Voltage Window Beyond 2.0 Volt. *Small Struct.*, 1: 2000020. <https://doi.org/10.1002/sstr.20200020>
- [19] M. R. R. Abdul-Aziz et al., "High Performance Supercapacitor Based on Laser Induced Graphene for Wearable Devices," in *IEEE Access*, vol. 8, pp. 200573-200580, 2020, doi: 10.1109/ACCESS.2020.3035828.
- [20] D. Yıldırım et al., "Full-Scale Physical Simulator of All SiC Traction Motor Drive With Onboard Supercapacitor ESS for Light-Rail Public Transportation," in *IEEE Transactions on Industrial Electronics*, vol. 67, no. 8, pp. 6290-6301, Aug. 2020, doi: 10.1109/TIE.2019.2934086.
- [21] S. Rani and Y. Sharma, "Fabrication of Binder-Free and High Energy Density Yarn Supercapacitor for Wearable Electronics," in *IEEE Transactions on Power Electronics*, vol. 37, no. 11, pp. 13022-13029, Nov. 2022, doi: 10.1109/TPEL.2022.3186958.
- [22] B. B. Beenarani and C. P. Sugumaran, "The Electrochemical Performance of Simple, Flexible and Highly Thermally Stable PVA-TiO₂ Nanocomposite in an All-Solid-State Supercapacitor," in *IEEE Transactions on Nanotechnology*, vol. 20, pp. 215-223, 2021, doi: 10.1109/TNANO.2021.3059524.
- [23] F. Xia, S. Xu, S. Li and X. Wang, "On-Chip High-Power Supply Unit: Micro Supercapacitor With Superb Capacitance Density and Fast Charge/Discharge Ability," in *IEEE Electron Device Letters*, vol. 42, no. 4, pp. 625-628, April 2021, doi: 10.1109/LED.2021.3063474.
- [24] P. Roy, J. He and Y. Liao, "Cost Minimization of Battery-Supercapacitor

- Hybrid Energy Storage for Hourly Dispatching Wind-Solar Hybrid Power System," in *IEEE Access*, vol. 8, pp. 210099-210115, 2020, doi: 10.1109/ACCESS.2020.3037149.
- [25] S. Perumal, A. L. L. Jarvis and M. Z. Gaffoor, "Effect of Graphite Precursor Flake Size on Energy Storage Capabilities of Graphene Oxide Supercapacitors," in *SAIEE Africa Research Journal*, vol. 112, no. 2, pp. 67-76, June 2021, doi: 10.23919/SAIEE.2021.9432895.
- [26] F. Naseri, E. Farjah, Z. Kazemi, E. Schaltz, T. Ghanbari and J. -L. Schanen, "Dynamic Stabilization of DC Traction Systems Using a Supercapacitor-Based Active Stabilizer With Model Predictive Control," in *IEEE Transactions on Transportation Electrification*, vol. 6, no. 1, pp. 228-240, March 2020, doi: 10.1109/TTE.2020.2964423.
- [27] E. Naderi, B. K. C., M. Ansari and A. Asrari, "Experimental Validation of a Hybrid Storage Framework to Cope With Fluctuating Power of Hybrid Renewable Energy-Based Systems," in *IEEE Transactions on Energy Conversion*, vol. 36, no. 3, pp. 1991-2001, Sept. 2021, doi: 10.1109/TEC.2021.3058550.
- [28] J. Vega and J. Lezama, "Design and Implementation of a Thermoelectric Energy Harvester with MPPT Algorithms and Supercapacitor," in *IEEE Latin America Transactions*, vol. 19, no. 01, pp. 163-170, January 2021, doi: 10.1109/TLA.2021.9423860.
- [29] R. A. S. Peña, A. Hijazi, P. Venet and F. Errigo, "Balancing Supercapacitor Voltages in Modular Bidirectional DC-DC Converter Circuits," in *IEEE Transactions on Power Electronics*, vol. 37, no. 1, pp. 137-149, Jan. 2022, doi: 10.1109/TPEL.2021.3093767.
- [30] Y. Zhao, W. Xie, Z. Fang and S. Liu, "A Parameters Identification Method of the Equivalent Circuit Model of the Supercapacitor Cell Module Based on Segmentation Optimization," in *IEEE Access*, vol. 8, pp. 92895-92906, 2020, doi: 10.1109/ACCESS.2020.2993285.
- [31] A. Morandi et al., "Characterization and Model Parameters of Large Commercial Supercapacitor Cells," in *IEEE Access*, vol. 9, pp. 20376-20390, 2021, doi: 10.1109/ACCESS.2021.3053626.
- [32] S. Mukhopadhyay, R. Dhaouadi, M. Takrouri and R. Dogga, "Supercapacitor Characterization Using Universal Adaptive Stabilization and Optimization," in *IEEE Open Journal of the Industrial Electronics Society*, vol. 1, pp. 166-183, 2020, doi: 10.1109/OJIES.2020.3008339.
- [33] S. Yesmin, I. Hussain, M. Devi, R. Dasgupta and S. S. Dhar, "Exploration of Cu/g-C₃N₄ Nanocomposites as a Cost-Effective High-Performance Asymmetric Supercapacitor Electrode Material," in *IEEE Transactions on Nanotechnology*, vol. 21, pp. 474-480, 2022, doi: 10.1109/TNANO.2022.3194097.
- [34] F. Martin Ibanez, I. Idrisov, F. Martin and A. Rujas, "Design Balancing Systems for Supercapacitors Based on Their Stochastic Model," in *IEEE Transactions on Energy Conversion*, vol. 35, no. 2, pp. 733-745, June 2020, doi: 10.1109/TEC.2020.2968364.
- [35] E. Mohammadi, R. Rasoulinezhad and G. Moschopoulos, "Using a Supercapacitor to Mitigate Battery Microcycles Due to Wind Shear and Tower Shadow Effects in Wind-Diesel Microgrids," in *IEEE Transactions on Smart Grid*, vol. 11, no. 5, pp. 3677-3689, Sept. 2020, doi: 10.1109/TSG.2020.2979140.
- [36] H. Li et al., "Pinning-Based Switching Control of Cyber-Physical Supercapacitor Energy Storage Systems," in *IEEE Transactions on Control Systems*

- Technology, vol. 28, no. 4, pp. 1520-1533, July 2020, doi: 10.1109/TCST.2019.2916039.
- [37] H. Li, X. Zhang, J. Peng, J. He, Z. Huang and J. Wang, "Cooperative CC–CV Charging of Supercapacitors Using Multicharger Systems," in IEEE Transactions on Industrial Electronics, vol. 67, no. 12, pp. 10497-10508, Dec. 2020, doi: 10.1109/TIE.2019.2962485.
- [38] Z. Zhong, Z. Yang, X. Fang, F. Lin and Z. Tian, "Hierarchical Optimization of an On-Board Supercapacitor Energy Storage System Considering Train Electric Braking Characteristics and System Loss," in IEEE Transactions on Vehicular Technology, vol. 69, no. 3, pp. 2576-2587, March 2020, doi: 10.1109/TVT.2020.2967467.
- [39] S. East and M. Cannon, "Optimal Power Allocation in Battery/Supercapacitor Electric Vehicles Using Convex Optimization," in IEEE Transactions on Vehicular Technology, vol. 69, no. 11, pp. 12751-12762, Nov. 2020, doi: 10.1109/TVT.2020.3023186.
- [40] H. Zhang, F. Zhang, L. Yang, Y. Gao and B. Jin, "Multi-Parameter Collaborative Power Prediction to Improve the Efficiency of Supercapacitor-Based Regenerative Braking System," in IEEE Transactions on Energy Conversion, vol. 36, no. 4, pp. 2612-2622, Dec. 2021, doi: 10.1109/TEC.2021.3074697.
- [41] Y. Yan, Q. Li, W. Huang and W. Chen, "Operation Optimization and Control Method Based on Optimal Energy and Hydrogen Consumption for the Fuel Cell/Supercapacitor Hybrid Tram," in IEEE Transactions on Industrial Electronics, vol. 68, no. 2, pp. 1342-1352, Feb. 2021, doi: 10.1109/TIE.2020.2967720.
- [42] F. Zhu, Z. Yang, Z. Zhao and F. Lin, "Two-Stage Synthetic Optimization of Supercapacitor-Based Energy Storage Systems, Traction Power Parameters and Train Operation in Urban Rail Transit," in IEEE Transactions on Vehicular Technology, vol. 70, no. 9, pp. 8590-8605, Sept. 2021, doi: 10.1109/TVT.2021.3100412.
- [43] T. Mesbahi, P. Bartholomeüs, N. Rizoug, R. Sadoun, F. Khenfri and P. L. Moigne, "Advanced Model of Hybrid Energy Storage System Integrating Lithium-Ion Battery and Supercapacitor for Electric Vehicle Applications," in IEEE Transactions on Industrial Electronics, vol. 68, no. 5, pp. 3962-3972, May 2021, doi: 10.1109/TIE.2020.2984426.
- [44] H. Miniguano, A. Barrado and A. Lázaro, "Li-Ion Battery and Supercapacitor Modeling for Electric Vehicles Based on Pulse – Pseudo Random Binary Sequence," in IEEE Transactions on Vehicular Technology, vol. 70, no. 11, pp. 11378-11389, Nov. 2021, doi: 10.1109/TVT.2021.3112284.
- [45] P. Nambisan and M. Khanra, "Optimal Energy Management of Battery Supercapacitor Aided Solar PV Powered Agricultural Feed Mill Using Pontryagin's Minimum Principle," in IEEE Transactions on Power Electronics, vol. 37, no. 2, pp. 2216-2225, Feb. 2022, doi: 10.1109/TPEL.2021.3104347.
- [46] M. Pacheco et al., "Enhancement of a Green Supercapacitor With a Hydrogel/Carbon Nanotubes-Based Electrolyte," in IEEE Transactions on Nanotechnology, vol. 19, pp. 711-718, 2020, doi: 10.1109/TNANO.2020.3019764.
- [47] P. Saha, S. Dey and M. Khanra, "Modeling and State-of-Charge Estimation of Supercapacitor Considering Leakage Effect," in IEEE Transactions on Industrial Electronics, vol. 67, no. 1, pp. 350-357, Jan. 2020, doi: 10.1109/TIE.2019.2897506.

- [48] S. Xu, F. Xia, Z. Li and X. Wang, "Wafer-Scale Fabrication and Encapsulation of Micro Supercapacitor," in IEEE Electron Device Letters, vol. 43, no. 3, pp. 474-477, March 2022, doi: 10.1109/LED.2022.3144578.
- [49] B. Pandit et al., "Two-Dimensional Hexagonal SnSe Nanosheets as Binder-Free Electrode Material for High-Performance Supercapacitors," in IEEE Transactions on Power Electronics, vol. 35, no. 11, pp. 11344-11351, Nov. 2020, doi: 10.1109/TPEL.2020.2989097.
- [50] S. Sundriyal, V. Shrivastav, P. Dubey, M. Singh, A. Deep and S. R. Dhakate, "Highly Porous Carbon From Azadirachta Indica Leaves and Uio-66 Derived Metal Oxide for Asymmetrical Supercapacitors," in IEEE Transactions on Nanotechnology, vol. 21, pp. 60-65, 2022, doi: 10.1109/TNANO.2022.3144367.