

A Heuristic Approach of Solving Real Life Problems Using Assignment and Transportation Model

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Abstract

In Real life, getting things from many supply sources to multiple destinations in a reasonable amount of time is a challenge. It is frequently done in order to solve a transportation difficulty. Here, the drivers must be assigned with efficiency, which can be accomplished via assignment, and the product must be brought to the destination in the shortest time possible, which can be accomplished through transportation. This study claims that all transportation challenges cannot be solved without the use of assignment. With numerical examples, this is clearly demonstrated..

Keywords: Transportation problems, supply, Demand, Assignment, optimization.

Introduction:

Models for transportation and assignment are mathematical procedures. The LPP (Simplified Methodology of Used Mathematical Problems) indicates that some aspects, such as optimal assignment of people to tasks, and delivery of commodities from many supply points in different directions, are unproductive. Assignments and transport models are two subgroups of more realistic response models that have been established. In the event of any demand for supply and supply barriers, the transportation model claims that the choice of routes between supply and demand is decided by the decrease of transportation costs. To suit

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particular demands, a good area unit has been shifted from the source collection (factory) to a set of destinations. The premise is that the product has been carried from several sources in different directions, lowering the cost of transportation or transportation. The objective is to establish supply obstacles at the lowest possible transportation cost. To achieve this goal, we must first comprehend the quantity of available supplies and, as a result, the amounts required. We also need to understand the location in order to calculate the cost of shipping one unit of commodities from the point of origin to the point of destination. The model is useful for making strategic decisions about optimal transportation routes and assigning the production of various plants to a large number of warehouses or distribution hubs. As a result, the transportation difficulty is that the various scales of the product, namely the various origins, are entirely different in that the transport price is minimum. In 1941, F.I. Hitchaxic proposed the basic transportation problem. However, it was only in 1951 that it was addressed optimally as a solution to a complex business problem, when St. George B. Dantzig applied the notion of applied math to the Transportation models. In all of these situations, transportation concerns occur. Its goal is to assist the company's upper management in determining how many units of a certain product should be delivered from each supply origin to each demand destination in order to satisfy the whole current demand for the company's product while lowering overall transportation costs. As a result, all modes of transportation include some form of assignment.

II. Mathematical form of transportation problem The transportation problem can be formulated as an LP problem.

Let $K_{ij}, i = 1 \dots m, j = 1 \dots n$ be the number of units transported from source i to destination j .

The LP problem is as follows Minimize $Z = \sum \sum T_{ij} K_{ij} \quad n \quad j = 1 \quad m \quad i = 1$ Subject to the constraints $\sum K_{ij} \leq S_i \quad n \quad j = 1$ For all $i \quad \sum K_{ij} \geq d_j \quad m \quad i = 1$ For all $j \quad K_{ij} \geq 0$.

II. Algorithm

(For a project) 1st step To begin, a matrix with an assignment issue is created. It is critical to have a balanced matrix; otherwise, it will be necessary to make an attempt to balance it by adding dummy rows or columns with zero entries.

Step 2 From a particular pricing matrix, a new matrix is created by subtracting the row's minimum component from all other parts in an equal row. Column-wise subtraction of the minimal element with its associated elements is performed inside the smaller matrix thus produced.

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Step 3: Talk about the zero point in the matrix. The summation is completed row-wise and column-wise by considering the zero of the (i,j) th place within the matrix. The maximum element value is determined from the resulting matrix, and zero value locations are assigned before the relevant row and column are eliminated. The technique described above is repeated for the smaller matrix until all of the rows and columns have been allocated. Step 4: If there is a tie for the highest maximum element, the highest maximum element with the lowest cost price is assigned. Step 5: Using the expression, calculate the total assignment cost. Total cost = $\sum \sum Cij Xi$.

III. Algorithm

(For the purpose of transportation) 1st step Construct the transportation problem's information matrix from the provided problem. We have a propensity to develop a balanced problem if it is imbalanced.

Step 2 Determine the minimum (maximum) component in each column, resulting in a table constructed by subtracting the minimum (maximum) cost in each column from each cost.

Step 3 Each column is to be discussed Observe zero (i,j) position and run the total number of rows and columns to zero to determine availability or demand to zero at most. Remove the appropriate rows or columns when availability or demand is satisfied. The left over table is then mentioned. The method is continued to the remaining table in anticipation of $m + n - 1$ cells are allotted and every one the availability and demand is satisfied.

Step 4 If there's tie within the maximum value of add of row and column, then apportion the zero that has minimum supply or demand.

Step 5 Repeat steps three and four until all the availability and demand is satisfied.

Step 6 Finally total minimum cost of the transportation is calculated by Total cost = $\sum \sum Cij Xij n j = 1 n i = 1$

IV. ALGORITHM (Combination of Assignment in Transportation).

To begin, a matrix with an assignment issue is created. It's critical to have a balanced matrix; if you don't, you'll have to make an effort to balance it by adding fake rows or columns with zero entries.

Step 2 Subtract the minimum component of the row from all or any distinct components from an equivalent row to create a new matrix from a given pricing matrix. Column-wise subtraction of the minimal component with its corresponding components is performed inside the reduced matrix thus produced.

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Step 3: Talk about the zero point in the matrix. The summation is performed row-wise and column-wise using the known position, taking into account the zero of the (i,j)th position within the matrix. When the matching row and column are eliminated, the most component value is known from the resulting matrix, and 0 value locations are allocated. The aforementioned procedure is repeated for the smaller matrix until all of the rows and columns have been allocated.

Step 4: If there is a tie with the same maximum element, the row's direct successor worth to zero is determined, as well as the most valuable component, and that row is allocated.

Step 5: Once you've acquired the assignment, you'll need to address the transportation issue. To begin, allocate for the allotted cells with the least amount of supply and demand. Allotted for the smallest value with the smallest supply/demand for the remaining empty cells. Step 6: Finally, the overall minimal cost is computed as the product of the cost and the associated supply or demand assigned value.

$$\text{Total cost} = \sum \sum C_{ij} X_{ij} \quad n_j = 1 \quad n_i = 1$$

IV. Numerical Example

A company has four plants 1,2,3,4 and four warehouses P,Q,R,S. The number of units available at the plants is 34,15,12 and 19 and the demand is 21,25,17 and 17 respectively. The unit cost of the transportation (mileage cost) is given by the toll table.

TABLE 1

	P	Q	R	S
S ₁	7	3	5	5
S ₂	5	5	7	6
S ₃	8	6	6	5
S ₄	6	1	6	4

find the allocation so that the total transportation cost is minimum.

Stage 1: Assignment(Using zero reduction method)

After Row Reduction and Column Reduction

TABLE 2

	P	Q	R	S		
S₁	4	8	0	1	2	
S₂	14	0	13	0	1	1
S₃	3		1		10	0 10 0
S₄	5		13	0	4	3

TABLE 3

	P	Q	R	S		
S₁	7	(6)	3	(6)	5	(17) 5 (5) 34
S₂	5	(15)	5		7	6 15
S₃	8		6		6	5 (12) 12
S₄	6		1	(19)	6	4 19
	21	25	17	17	80	

First allocate the Assignment $S_1 \rightarrow R, S_2 \rightarrow P, S_3 \rightarrow S$ and $S_4 \rightarrow Q$ in the transportation table, then the remaining is allocated to minimum unallocated cells. Hence combining Assignment in transportation, we are able to obtain an optimal solution in single table. Time comparison chart of Zero's Reduction Method with Hungarian and Modi Method

Conclusion:

This analytical study deals with a direct way for determining transportation problems. This research may be used to any situation. This is a systematic technique of offering a cost-effective resolution in fewer stages; also, this methodology is comparable to MODI methodology in that degeneracy is avoided. As a result, we've come up with a novel

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algorithm for merging assignments in Transportation. As a result, it's evident that Assignment's aid is required for transportation. As a result, Assignment and Transportation are inextricably linked.

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