

Cycle Related K^{th} Fibonacci Prime Labeling Of Graphs

K. Periasamy¹ and K. Venugopal²

¹ Guest Lecturer, P.G. and Research Department of Mathematics, Dr. Kalaignar Government Arts college, Affiliated to Bharathidasan University, Tiruchirappalli, India.

² Assistant Professor, P.G. and Research Department of Mathematics, Dr. Kalaignar Government Arts college, Kulithalai- 639120, Affiliated to Bharathidasan University, Tiruchirappalli, India.

¹kpsperiasamy87@gmail.com

²drvenugopal2013@gmail.com

ABSTRACT :

In this paper, we investigate the k^{th} fibonacci prime labeling of two new families of graphs, which are a graph G is obtained by joining two cycles C_n and C_m by a path P_s and a graph G is obtained by joining two cycles C_n and C_m by a triangular snake T_s .

Keywords – fibonacci number, fibonacci prime labeling, fibonacci prime graph, triangular snake, k^{th} fibonacci prime graph.

1. INTRODUCTION

By a graph, we mean a finite, undirected graph without loops and multiple edges, for terms not defined here, we refer to Bondy and Murthy [1]. For standard terminology and notations related to number theory we refer to Burton [2] and graph labeling, we refer to Gallian [3]. The notion of prime labeling for graphs originated with Roger Entringer and was introduced in a paper by Tout et al. [6]. In [7], Vaidya et al. introduced the concept of k -prime labeling of graph. Sekar et al. introduced the concept of Fibonacci Prime Labeling of Graphs in [5]. Periasamy et al. introduced k^{th} Fibonacci Prime Labeling of Graphs and k^{th} Fibonacci Prime Labeling of some standard graphs are discussed in [4]. In this paper, we present the k^{th} Fibonacci prime labeling of a graph G is obtained by joining two cycles C_n and C_m by a path P_s and a graph G is obtained by joining two cycles C_n and C_m by a triangular snake T_s .

Definition :1.1 A graph labeling is the assignment of unique identifiers to the edges and vertices of a graph.

Definition :1.2 Let $G = (V,E)$ be a graph with n vertices. A function $f : V(G) \rightarrow \{1,2,3,\dots,n\}$ is said to be a prime labeling, if it is bijective and for every pair of adjacent vertices u and v , $\gcd(f(u),f(v)) = 1$. A graph which admits prime labeling is called a prime graph.

Definition : 1.3 The Fibonacci number f_n is defined recursively by the equations $f_1 = 1, f_2 = 1,$

$f_{n+1} = f_n + f_{n-1}$ ($n \geq 2$). Then $\gcd(f_n, f_{n-1}) = 1$ and $\gcd(f_n, f_{n+1}) = 1$ for all $n \geq 1$.

Definition : 1.4 A Fibonacci prime labeling of a graph $G = (V, E)$ with $|V(G)| = n$ is an injective function $g : V(G) \rightarrow \{f_2, f_3, \dots, f_{n+1}\}$, where f_n is the n^{th} Fibonacci number, that induces a function $g^* : E(G) \rightarrow \mathbb{N}$ defined by $g^*(uv) = \gcd\{g(u), g(v)\} = 1, \forall uv \in E(G)$. The graph admits a Fibonacci prime labeling and is called a Fibonacci prime graph.

Definition : 1.5 A k^{th} Fibonacci prime labeling of a graph $G = (V, E)$ with $|V(G)| = n$ is an injective function $g : V(G) \rightarrow \{f_k, f_{k+1}, \dots, f_{k+n-1}\}$, where f_k is the k^{th} Fibonacci number, that induces a function $g^* : E(G) \rightarrow \mathbb{N}$ defined by $g^*(uv) = \gcd\{g(u), g(v)\} = 1, \forall uv \in E(G)$. The graph admits a k^{th} Fibonacci prime labeling and is called a k^{th} Fibonacci prime graph.

Remark : 1.1 A 2^{nd} Fibonacci prime graph is called Fibonacci prime graph.

2. Main Results

Theorem 2.1

The graph G is obtained by joining two cycles C_n and C_m by a path P_s is a k^{th} Fibonacci prime graph $n, m \geq 3, k, s \geq 2$.

Proof.

The graph G is obtained by joining two cycles C_n and C_m by a path P_s .

Let v_1, v_2, \dots, v_n be the vertices of the cycle C_n , w_1, w_2, \dots, w_m be the vertices of the cycle C_m and u_1, u_2, \dots, u_s be the vertices of the path P_s with $u_1 = v_1$ and $u_s = w_1$.

The edge set $E(G) = \{v_i v_{i+1} \mid 1 \leq i \leq n-1\} \cup \{v_n v_1\} \cup \{v_1 u_2\} \cup \{u_i u_{i+1} \mid 2 \leq i \leq s-2\} \cup \{u_{s-1} w_1\} \cup \{w_i w_{i+1} \mid 1 \leq i \leq m-1\} \cup \{w_m w_1\}$.

Then $|V(G)| = n+s+m-2$ and $|E(G)| = n+s+m-1$.

Define the mapping $g : V(G) \rightarrow \{f_k, f_{k+1}, \dots, f_{k+n+s+m-3}\}$ as follows

Case 1 : n is odd.

$$g(v_i) = f_{k+n-2i+1}, \text{ for } 1 \leq i \leq \frac{n+1}{2}$$

$$g(v_i) = f_{k-n+2i-2}, \text{ for } \frac{n+3}{2} \leq i \leq n$$

$$g(u_i) = f_{k+n+i-2}, \text{ for } 2 \leq i \leq s-1$$

Case 1(a) : m is odd.

$$g(w_i) = f_{k+n+s+2i-4}, \text{ for } 1 \leq i \leq \frac{m+1}{2}$$

$$g(w_i) = f_{k+n+s+2m-2i-1}, \text{ for } \frac{m+3}{2} \leq i \leq m$$

Case 1(b) : m is even.

$$g(w_i) = f_{k+n+s+2i-4}, \text{ for } 1 \leq i \leq \frac{m}{2}$$

$$g(w_i) = f_{k+n+s+2m-2i-1}, \text{ for } \frac{m+2}{2} \leq i \leq m$$

Then the induced function $g^* : E(G) \rightarrow N$ is defined by

$$g^*(xy) = \gcd\{g(x),g(y)\} \quad \forall xy \in E(G).$$

Now,

$$\gcd\{g(v_i),g(v_{i+1})\} = \gcd\{f_{k+n-2i+1}, f_{k+n-2i-1}\} = 1, 1 \leq i \leq \frac{n-1}{2}$$

$$\gcd\{g(v_i),g(v_{i+1})\} = \gcd\{f_k, f_{k+1}\} = 1, i = \frac{n+1}{2}$$

$$\gcd\{g(v_i),g(v_{i+1})\} = \gcd\{f_{k-n+2i-2}, f_{k-n+2i}\} = 1, \frac{n+3}{2} \leq i \leq n-1$$

$$\gcd\{g(v_n),g(v_1)\} = \gcd\{f_{k+n-2}, f_{k+n-1}\} = 1$$

$$\gcd\{g(v_1),g(u_2)\} = \gcd\{f_{k+n-1}, f_{k+n}\} = 1$$

$$\gcd\{g(u_i),g(u_{i+1})\} = \gcd\{f_{k+n+i-2}, f_{k+n+i-1}\} = 1, 2 \leq i \leq s-1$$

$$\gcd\{g(u_s),g(w_1)\} = \gcd\{f_{k+n+s-3}, f_{k+n+s-2}\} = 1$$

when m is odd

$$\gcd\{g(w_i),g(w_{i+1})\} = \gcd\{f_{k+n+s+2i-4}, f_{k+n+s+2i-2}\} = 1, 1 \leq i \leq \frac{m-1}{2}$$

$$\gcd\{g(w_i),g(w_{i+1})\} = \gcd\{f_{k+n+s+m-3}, f_{k+n+s+m-4}\} = 1, i = \frac{m+1}{2}$$

$$\gcd\{g(w_i),g(w_{i+1})\} = \gcd\{f_{k+n+s+2m-2i-1}, f_{k+n+s+2m-2i-3}\} = 1, \frac{m+3}{2} \leq i \leq m-1$$

$$\gcd\{g(w_n),g(w_1)\} = \gcd\{f_{k+n+s-1}, f_{k+n+s-2}\} = 1$$

when m is even

$$\gcd\{g(w_i),g(w_{i+1})\} = \gcd\{f_{k+n+s+2i-4}, f_{k+n+s+2i-2}\} = 1, 1 \leq i \leq \frac{m-2}{2}$$

$$\gcd\{g(w_i),g(w_{i+1})\} = \gcd\{f_{k+n+s+m-4}, f_{k+n+s+m-3}\} = 1, i = \frac{m}{2}$$

$$\gcd\{g(w_i),g(w_{i+1})\} = \gcd\{f_{k+n+s+2m-2i-1}, f_{k+n+s+2m-2i-3}\} = 1, \frac{m+2}{2} \leq i \leq m-1$$

$$\gcd\{g(w_n),g(w_1)\} = \gcd\{f_{k+n+s-1}, f_{k+n+s-2}\} = 1$$

Thus $g^*(xy) = \gcd\{f(x),f(y)\} = 1, \forall xy \in E(G)$.

Case 2 : n is even.

$$g(v_i) = f_{k+n-2i+1}, \text{ for } 1 \leq i \leq \frac{n}{2}$$

$$g(v_i) = f_{k-n+2i-2}, \text{ for } \frac{n+2}{2} \leq i \leq n$$

$$g(u_i) = f_{k+n+i-2}, \text{ for } 2 \leq i \leq s-1$$

Case 2(a) : m is odd.

$$g(w_i) = f_{k+n+s+2i-4}, \text{ for } 1 \leq i \leq \frac{m+1}{2}$$

$$g(w_i) = f_{k+n+s+2m-2i-1}, \text{ for } \frac{m+3}{2} \leq i \leq m$$

Case 2(b) : m is even.

$$g(w_i) = f_{k+n+s+2i-4}, \text{ for } 1 \leq i \leq \frac{m}{2}$$

$$g(w_i) = f_{k+n+s+2m-2i-1}, \text{ for } \frac{m+2}{2} \leq i \leq m$$

Then the induced function $g^* : E(G) \rightarrow N$ is defined by

$$g^*(xy) = \gcd\{g(x),g(y)\} \quad \forall xy \in E(G).$$

Now,

$$\gcd\{g(v_i),g(v_{i+1})\} = \gcd\{f_{k+n-2i+1}, f_{k+n-2i-1}\} = 1, 1 \leq i \leq \frac{n-2}{2}$$

$$\gcd\{g(v_i),g(v_{i+1})\} = \gcd\{f_{k+1}, f_k\} = 1, i = \frac{n}{2}$$

$$\gcd\{g(v_i),g(v_{i+1})\} = \gcd\{f_{k-n+2i-2}, f_{k-n+2i}\} = 1, \frac{n+2}{2} \leq i \leq n-1$$

$$\gcd\{g(v_n),g(v_1)\} = \gcd\{f_{k+n-2}, f_{k+n-1}\} = 1$$

$$\gcd\{g(v_1),g(u_2)\} = \gcd\{f_{k+n-1}, f_{k+n}\} = 1$$

$$\gcd\{g(u_i),g(u_{i+1})\} = \gcd\{f_{k+n+i-2}, f_{k+n+i-1}\} = 1, 2 \leq i \leq s-1$$

$$\gcd\{g(u_s),g(w_1)\} = \gcd\{f_{k+n+s-3}, f_{k+n+s-2}\} = 1$$

when m is odd

$$\gcd\{g(w_i),g(w_{i+1})\} = \gcd\{f_{k+n+s+2i-4}, f_{k+n+s+2i-2}\} = 1, 1 \leq i \leq \frac{m-1}{2}$$

$$\gcd\{g(w_i),g(w_{i+1})\} = \gcd\{f_{k+n+s+m-3}, f_{k+n+s+m-4}\} = 1, i = \frac{m+1}{2}$$

$$\gcd\{g(w_i),g(w_{i+1})\} = \gcd\{f_{k+n+s+2m-2i-1}, f_{k+n+s+2m-2i-3}\} = 1, \frac{m+3}{2} \leq i \leq m-1$$

$$\gcd\{g(w_n),g(w_1)\} = \gcd\{f_{k+n+s-1}, f_{k+n+s-2}\} = 1$$

when m is even

$$\gcd\{g(w_i),g(w_{i+1})\} = \gcd\{f_{k+n+s+2i-4}, f_{k+n+s+2i-2}\} = 1, 1 \leq i \leq \frac{m-2}{2}$$

$$\gcd\{g(w_i),g(w_{i+1})\} = \gcd\{f_{k+n+s+m-4}, f_{k+n+s+m-3}\} = 1, i = \frac{m}{2}$$

$$\gcd\{g(w_i),g(w_{i+1})\} = \gcd\{f_{k+n+s+2m-2i-1}, f_{k+n+s+2m-2i-3}\} = 1, \frac{m+2}{2} \leq i \leq m-1$$

$$\gcd\{g(w_n),g(w_1)\} = \gcd\{f_{k+n+s-1}, f_{k+n+s-2}\} = 1$$

Thus $g^*(xy) = \gcd\{f(x),f(y)\} = 1, \forall xy \in E(G).$

Therefore, the graph G is obtained by joining two cycles C_n and C_m by a path P_s is a k^{th} Fibonacci prime graph $n, m \geq 3, k, s \geq 2$.

Illustration 2.1

The graph G is obtained by joining two cycles C_6 and C_7 by a path P_7 and its 3rd Fibonacci prime labeling are shown in figure 2.1.

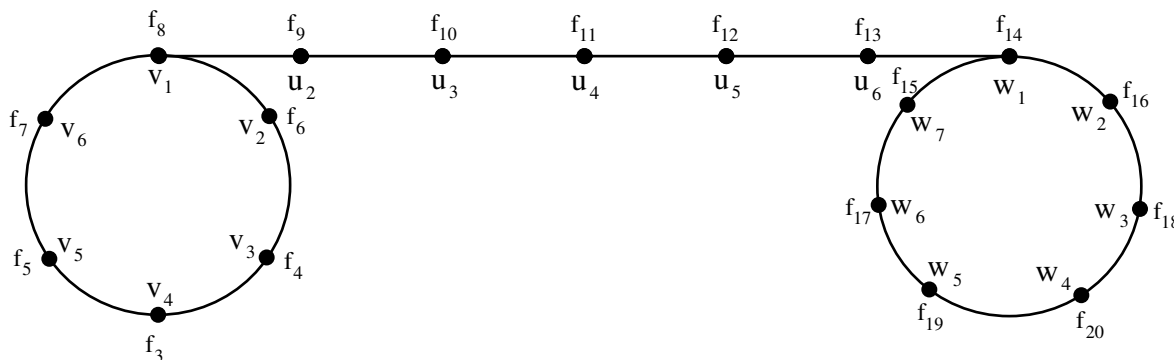


Figure 2.1 Graph G is obtained by joining two cycles C_6 and C_7 by a path P_7 is 3rd Fibonacci prime graph

Theorem 2.2

The graph G is obtained by joining two cycles C_n and C_m by a triangular snake T_s is a k^{th} Fibonacci prime graph $n, m \geq 3, k, s \geq 2$.

Proof.

The graph G is obtained by joining two cycles C_n and C_m by a triangular snake T_s .

Let v_1, v_2, \dots, v_n be the vertices of the cycle C_n , w_1, w_2, \dots, w_m be the vertices of the cycle C_m and $x_1, x_2, \dots, x_s, y_1, y_2, \dots, y_{s-1}$ be the vertices of the triangular snake T_s with $x_1 = v_1$ and $x_s = w_1$.

$$\begin{aligned} \text{The edge set } E(G) = & \{v_i v_{i+1} \mid 1 \leq i \leq n-1\} \cup \{v_n v_1\} \cup \{v_1 x_2\} \cup \{v_1 y_1\} \cup \\ & \{x_i x_{i+1} \mid 2 \leq i \leq s-2\} \cup \{x_i y_i \mid 2 \leq i \leq s-1\} \cup \{y_i x_{i+1} \mid 1 \leq i \leq s-2\} \cup \{x_{s-1} w_1\} \cup \{y_{s-1} w_1\} \cup \\ & \{w_i w_{i+1} \mid 1 \leq i \leq m-1\} \cup \{w_m w_1\}. \end{aligned}$$

Then $|V(G)| = n+2s+m-3$ and $|E(G)| = n+3s+m-3$.

Define the mapping $g : V(G) \rightarrow \{f_k, f_{k+1}, \dots, f_{k+n+2s+m-4}\}$ as follows

Case 1 : n is odd.

$$g(v_i) = f_{k+n-2i+1}, \text{ for } 1 \leq i \leq \frac{n+1}{2}$$

$$g(v_i) = f_{k-n+2i-2}, \text{ for } \frac{n+3}{2} \leq i \leq n$$

$$g(x_i) = f_{k+n+2i-3}, \text{ for } 2 \leq i \leq s-1$$

$$g(y_i) = f_{k+n+2i-2}, \text{ for } 1 \leq i \leq s-1$$

Case 1(a) : m is odd.

$$g(w_i) = f_{k+n+2s+2i-5}, \text{ for } 1 \leq i \leq \frac{m+1}{2}$$

$$g(w_i) = f_{k+n+2s+2m-2i-2}, \text{ for } \frac{m+3}{2} \leq i \leq m$$

Case 1(b) : m is even.

$$g(w_i) = f_{k+n+2s+2i-5}, \text{ for } 1 \leq i \leq \frac{m}{2}$$

$$g(w_i) = f_{k+n+2s+2m-2i-2}, \text{ for } \frac{m+2}{2} \leq i \leq m$$

Then the induced function $g^* : E(G) \rightarrow N$ is defined by

$$g^*(xy) = \gcd\{g(x), g(y)\} \quad \forall xy \in E(G).$$

Now,

$$\gcd\{g(v_i), g(v_{i+1})\} = \gcd\{f_{k+n-2i+1}, f_{k+n-2i-1}\} = 1, \quad 1 \leq i \leq \frac{n-1}{2}$$

$$\gcd\{g(v_i), g(v_{i+1})\} = \gcd\{f_k, f_{k+1}\} = 1, \quad i = \frac{n+1}{2}$$

$$\gcd\{g(v_i), g(v_{i+1})\} = \gcd\{f_{k-n+2i-2}, f_{k-n+2i}\} = 1, \quad \frac{n+3}{2} \leq i \leq n-1$$

$$\gcd\{g(v_n), g(v_1)\} = \gcd\{f_{k+n-2}, f_{k+n-1}\} = 1$$

$$\gcd\{g(v_1), g(x_2)\} = \gcd\{f_{k+n-1}, f_{k+n+1}\} = 1$$

$$\gcd\{g(v_1), g(y_1)\} = \gcd\{f_{k+n-1}, f_{k+n}\} = 1$$

$$\gcd\{g(x_i), g(x_{i+1})\} = \gcd\{f_{k+n+2i-3}, f_{k+n+2i-1}\} = 1, \quad 2 \leq i \leq s-1$$

$$\gcd\{g(x_i), g(y_i)\} = \gcd\{f_{k+n+2i-3}, f_{k+n+2i-2}\} = 1, \quad 2 \leq i \leq s-1$$

$$\gcd\{g(y_i), g(x_{i+1})\} = \gcd\{f_{k+n+2i-2}, f_{k+n+2i-1}\} = 1, \quad 1 \leq i \leq s-1$$

$$\gcd\{g(x_{s-1}), g(w_1)\} = \gcd\{f_{k+n+s-4}, f_{k+n+2s-3}\} = 1$$

$$\gcd\{g(y_{s-1}), g(w_1)\} = \gcd\{f_{k+n+s-5}, f_{k+n+2s-3}\} = 1$$

when m is odd

$$\gcd\{g(w_i), g(w_{i+1})\} = \gcd\{f_{k+n+2s+2i-5}, f_{k+n+2s+2i-3}\} = 1, \quad 1 \leq i \leq \frac{m-1}{2}$$

$$\gcd\{g(w_i), g(w_{i+1})\} = \gcd\{f_{k+n+2s+m-4}, f_{k+n+2s+m-5}\} = 1, \quad i = \frac{m+1}{2}$$

$$\gcd\{g(w_i), g(w_{i+1})\} = \gcd\{f_{k+n+2s+2m-2i-2}, f_{k+n+2s+2m-2i-4}\} = 1, \quad \frac{m+3}{2} \leq i \leq m-1$$

$$\gcd\{g(w_n), g(w_1)\} = \gcd\{f_{k+n+2s-2}, f_{k+n+2s-3}\} = 1$$

when m is even

$$\gcd\{g(w_i), g(w_{i+1})\} = \gcd\{f_{k+n+2s+2i-5}, f_{k+n+2s+2i-3}\} = 1, \quad 1 \leq i \leq \frac{m-2}{2}$$

$$\gcd\{g(w_i),g(w_{i+1})\} = \gcd\{f_{k+n+2s+m-5}, f_{k+n+2s+m-4}\} = 1, i = \frac{m}{2}$$

$$\gcd\{g(w_i),g(w_{i+1})\} = \gcd\{f_{k+n+2s+2m-2i-2}, f_{k+n+2s+2m-2i-4}\} = 1, \frac{m+2}{2} \leq i \leq m-1$$

$$\gcd\{g(w_n),g(w_1)\} = \gcd\{f_{k+n+2s-2}, f_{k+n+2s-3}\} = 1$$

Thus $g^*(xy) = \gcd\{f(x),f(y)\} = 1, \forall xy \in E(G)$.

Case 2 : n is even.

$$g(v_i) = f_{k+n-2i+1}, \text{ for } 1 \leq i \leq \frac{n}{2}$$

$$g(v_i) = f_{k-n+2i-2}, \text{ for } \frac{n+2}{2} \leq i \leq n$$

$$g(x_i) = f_{k+n+2i-3}, \text{ for } 2 \leq i \leq s-1$$

$$g(y_i) = f_{k+n+2i-2}, \text{ for } 1 \leq i \leq s-1$$

Case 2(a) : m is odd.

$$g(w_i) = f_{k+n+2s+2i-5}, \text{ for } 1 \leq i \leq \frac{m+1}{2}$$

$$g(w_i) = f_{k+n+2s+2m-2i-2}, \text{ for } \frac{m+3}{2} \leq i \leq m$$

Case 2(b) : m is even.

$$g(w_i) = f_{k+n+2s+2i-5}, \text{ for } 1 \leq i \leq \frac{m}{2}$$

$$g(w_i) = f_{k+n+2s+2m-2i-2}, \text{ for } \frac{m+2}{2} \leq i \leq m$$

Then the induced function $g^* : E(G) \rightarrow N$ is defined by

$$g^*(xy) = \gcd\{g(x),g(y)\} \forall xy \in E(G).$$

Now,

$$\gcd\{g(v_i),g(v_{i+1})\} = \gcd\{f_{k+n-2i+1}, f_{k+n-2i-1}\} = 1, 1 \leq i \leq \frac{n-2}{2}$$

$$\gcd\{g(v_i),g(v_{i+1})\} = \gcd\{f_{k+1}, f_k\} = 1, i = \frac{n}{2}$$

$$\gcd\{g(v_i),g(v_{i+1})\} = \gcd\{f_{k-n+2i-2}, f_{k-n+2i}\} = 1, \frac{n+2}{2} \leq i \leq n-1$$

$$\gcd\{g(v_n),g(v_1)\} = \gcd\{f_{k+n-2}, f_{k+n-1}\} = 1$$

$$\gcd\{g(v_1),g(x_2)\} = \gcd\{f_{k+n-1}, f_{k+n+1}\} = 1$$

$$\gcd\{g(v_1),g(y_1)\} = \gcd\{f_{k+n-1}, f_{k+n}\} = 1$$

$$\gcd\{g(x_i),g(x_{i+1})\} = \gcd\{f_{k+n+2i-3}, f_{k+n+2i-1}\} = 1, 2 \leq i \leq s-1$$

$$\gcd\{g(x_i),g(y_i)\} = \gcd\{f_{k+n+2i-3}, f_{k+n+2i-2}\} = 1, 2 \leq i \leq s-1$$

$$\gcd\{g(y_i),g(x_{i+1})\} = \gcd\{f_{k+n+2i-2}, f_{k+n+2i-1}\} = 1, 1 \leq i \leq s-1$$

$$\gcd\{g(x_{s-1}),g(w_1)\} = \gcd\{f_{k+n+s-4}, f_{k+n+2s-3}\} = 1$$

$$\gcd\{g(y_{s-1}),g(w_1)\} = \gcd\{f_{k+n+s-5}, f_{k+n+2s-3}\} = 1$$

when m is odd

$$\gcd\{g(w_i),g(w_{i+1})\} = \gcd\{f_{k+n+2s+2i-5}, f_{k+n+2s+2i-3}\} = 1, 1 \leq i \leq \frac{m-1}{2}$$

$$\gcd\{g(w_i),g(w_{i+1})\} = \gcd\{f_{k+n+2s+m-4}, f_{k+n+2s+m-5}\} = 1, i = \frac{m+1}{2}$$

$$\gcd\{g(w_i),g(w_{i+1})\} = \gcd\{f_{k+n+2s+2m-2i-2}, f_{k+n+2s+2m-2i-4}\} = 1, \frac{m+3}{2} \leq i \leq m-1$$

$$\gcd\{g(w_n),g(w_1)\} = \gcd\{f_{k+n+2s-2}, f_{k+n+2s-3}\} = 1$$

when m is even

$$\gcd\{g(w_i),g(w_{i+1})\} = \gcd\{f_{k+n+2s+2i-5}, f_{k+n+2s+2i-3}\} = 1, 1 \leq i \leq \frac{m-2}{2}$$

$$\gcd\{g(w_i),g(w_{i+1})\} = \gcd\{f_{k+n+2s+m-5}, f_{k+n+2s+m-4}\} = 1, i = \frac{m}{2}$$

$$\gcd\{g(w_i),g(w_{i+1})\} = \gcd\{f_{k+n+2s+2m-2i-2}, f_{k+n+2s+2m-2i-4}\} = 1, \frac{m+2}{2} \leq i \leq m-1$$

$$\gcd\{g(w_n),g(w_1)\} = \gcd\{f_{k+n+2s-2}, f_{k+n+2s-3}\} = 1$$

Thus $g^*(xy) = \gcd\{f(x),f(y)\} = 1, \forall xy \in E(G)$.

Therefore, the graph G is obtained by joining two cycles C_n and C_m by a triangular snake T_s is a k^{th} Fibonacci prime graph $n,m \geq 3, k,s \geq 2$.

Illustration 2.2

The graph G is obtained by joining two cycles C_7 and C_6 by a triangular snake T_5 and its 5th Fibonacci prime labeling are shown in figure 2.2.

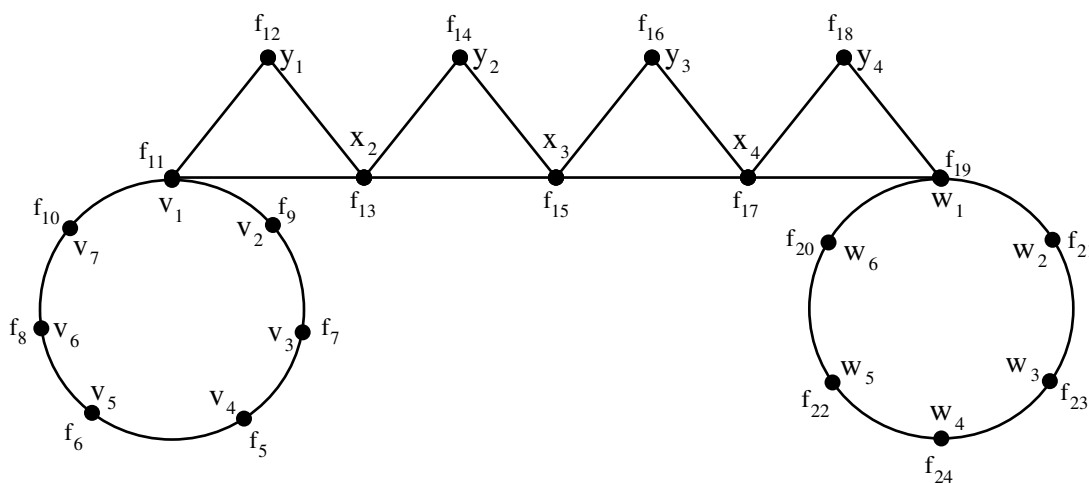


Figure 2.2 Graph G is obtained by joining two cycles C_7 and C_6 by a triangular snake T_5 is 5^{th} Fibonacci prime graph

3. CONCLUSION

In this paper, the k^{th} Fibonacci prime labeling of a graph G is obtained by joining two cycles C_n and C_m by a path P_s and a graph G is obtained by joining two cycles C_n and C_m by a triangular snake T_s are presented.

REFERENCES

- [1] J.A. Bondy and U.S.R. Murthy, Graph Theory and Application (North Holland). New York (1976).
- [2] D.M. Burton, Elementary Number Theory, Second Edition, Wm. C. Brown Company Publishers, (1980).
- [3] J.A. Gallian, A Dynamic Survey of Graph Labeling, The Electronic Journal of Combinatorics, 16(2021), 147, #DS6.
- [4] K. Periasamy, K. Venugopal and P. Lawrence Rozario Raj, k^{th} Fibonacci Prime Labeling of Graphs, International Journal of Mathematics Trends and Technology, 68(5), (2022), 61-67.
- [5] C. Sekar and S. Chandrakala, Fibonacci Prime Labeling of Graphs, International Journal of Creative Research Thoughts, 6(2), (2018), 995-1001.
- [6] A.N. Tout.A, Dabboucy and K. Howalla, Prime Labeling of Graphs, Nat.Acad .Sci letters 11 (1982) 365-368.
- [7] S. K. Vaidya and U. M. Prajapati, Some Results on Prime and k-Prime Labeling, J. Math. Research, 3(1), (2011), 66-75.